## Computer Science \& IT

## Compiler Design

## SHORT NOTES

## 푸미이미I!

## Short Notes — COMPILER DESIGN

- Definition: It converts high level language to low level language.

- High Level Language can perform more than one operation in single statement.
- Analysis and synthetic model of compiler:

- There are 6 phases of the compiler.


## 1. Lexical Analyzer:

Program of DFA, it checks for spelling mistakes of the program.
2. Syntax Analyzer :

It checks grammatical errors of the program. (Parser)

* Parser is a DPDA.

3. Semantic Analyzer:

Checks for meaning of the program.
[Eg. Type miss match, stack overflow]

* w/o Error handler, compiler can still work.


## 4. Intermediate Code generator :

This phase is used to make the work of next 2 phases much easier.
Enforces reusability and portability.
5. Code Optimization :

1. Loop invariant construction
2. Common sub expression elimination
3. Strength Reduction
4. Function in Lining
5. Dead code elimination

## 6. Symbol Table:

1. Data about data (meta data)
2. Date structure used by compiler and shared by all the phases.

* w/o symbol table compiler cannot work.
- CD - Grammar
$\Rightarrow$ In compiler we only use: Type - 2 (CFG) and Type - 3 (RG) Grammers.
$\Rightarrow$ Compiler $=$ Program of Grammar
$\Rightarrow$ Compiler $=$ Membership Algorithm
* Every programming Language is CSG. (CSL)
- Parse Tree and Syntax Tree :

$$
\begin{aligned}
& \mathrm{G}: \mathrm{E} \rightarrow \mathrm{E}+\mathrm{T} / \mathrm{T} \rightarrow \mathrm{E} \rightarrow \mathrm{~T}+\mathrm{T} \rightarrow \mathrm{~T}+\mathrm{T} \rightarrow \mathrm{~T} * \mathrm{~F}+\mathrm{T} \rightarrow \mathrm{~F} * \mathrm{~F}+\mathrm{T} \\
& \mathrm{~T} \rightarrow \mathrm{~T} * \mathrm{~F} \mid \mathrm{F} \rightarrow 2 * \mathrm{~F}+\mathrm{T} \rightarrow 2 * 3+\mathrm{T} \rightarrow 2 * 3+\mathrm{F}
\end{aligned}
$$



* To check the priority / Associativity :

Randomly derive till you have enough operations, then check which one done first.

* If priority of 2 operators is same and both are Left and Right associative $\rightarrow$ Ambiguous Grammar.
[USELESS]
- Type of item in Bottom up : [CD - Parser]

- CD - Syntax Analysis Parsing

Grammatical errors are checked with the help of parsers.

[^0]

- Mathematical Model of Parser:

* Parsers generate parse tree, for a given string by the given grammar.
- Top down parser (LL (1)):
* It uses LMD and is equivalent to DFS in Graph.
- Algorithm to construct parsing table :

1. Remove Left Recursion if any.
2. Remove Left Factoring if any. [Remove common prefix.]
3. Find $1^{\text {st }}$ and follow set.
4. Construct the Table.

* If we increase the look ahead symbol:
$\rightarrow$ strength of parser $\uparrow$
$\rightarrow$ complexity of parser $\uparrow$
* [ Due to common prefix: Back track]
[ Due to left Recursion : $\infty$ RCC.]

Removal of common Prefix : (Left factor).

1. $\mathrm{S} \rightarrow \mathrm{a}|\underline{a b}| \underline{a} \mathrm{~A}$
$\Rightarrow S \rightarrow a Y$
$\mathrm{Y} \rightarrow \in \mathrm{B} \mid \mathrm{A}$.

$$
\text { 2. } \begin{aligned}
\mathrm{A} & \rightarrow \underline{\mathrm{ab}} \mathrm{~A}|\underline{\mathrm{a}} \mathrm{~A}| \mathrm{b} . \\
\Rightarrow \mathrm{A} & \rightarrow \mathrm{ax}|\mathrm{~b}| \mathrm{A} \rightarrow \mathrm{Ax} \mid \mathrm{b} \\
\mathrm{X} & \rightarrow \mathrm{bA}|\mathrm{~A}| \mathrm{x} \rightarrow \underline{\mathrm{~b}} \mathrm{~A}|\mathrm{ax}| \underline{\mathrm{b}}
\end{aligned}
$$

* Indirect common perfix

$$
\begin{aligned}
\Rightarrow \mathrm{A} & \rightarrow \mathrm{ax} \mid \mathrm{b} \\
\mathrm{x} & \rightarrow \mathrm{ax} \mid \mathrm{bY} \\
\mathrm{Y} & \rightarrow \mathrm{~A} \mid \in
\end{aligned}
$$

- First and Follow:
$\circ$ First set $\rightarrow$ The extreme Left terminal from which the string of that variable starts.
* It never contains variables, but may contain ' $\epsilon$ '.
* We can always find the first of any variable.
- Follow set $\rightarrow$ Follow set contains terminals and $\$$.

It can never contain variable and " $\epsilon$ ".
How to find follow set?

1. Include $\$$ in follow of start variable.
2. If production is of type $\rightarrow$
$A \rightarrow a B \beta[a, \beta \rightarrow$ strings of grammar symbol.]

$$
\text { follow }(B)=\text { first }(\beta)
$$

If, $\beta \xrightarrow{*} \in$, ie $A \rightarrow \alpha \beta$, then follow $(B)=$ follow $(A)$
Production Like $: A \longrightarrow \mathbf{a A}_{\boldsymbol{A}}$ gives No follow set.

- Examples of first and follow set :

1. 

$S \rightarrow A B \mid C D$
$A \rightarrow a A \mid a$
$B \rightarrow b B \mid b$
$\mathrm{C} \rightarrow \mathrm{cC} \mid \mathrm{c}$
$\mathrm{D} \rightarrow \mathrm{dD} \mid \mathrm{d}$

|  | First | Follow |
| :---: | :---: | :---: |
| S | a,c | \$ |
| A | A | b |
| B | B | $\$$ |
| C | C | d |
| D | D | $\$$ |

- Entry into Table : Top down :

1. No of rows $=$ No of unique variables in Grammar.
2. No. of columns $=$ [Terminals $+\$]$
3. For a variable (ROW) fill the column (terminal) if it is there in its first's w/o the production reqd.
4. If $\epsilon$ is in first put $V \rightarrow \epsilon$ under $\$$ and its follows.

* If any cell has multiple times, then it not possible to have $\operatorname{LL}(1)$ parser. Since that will be ambiguous.
* [In top down we do : derivation]
[In Bottom up we do : Reduction]

2. Construct $\operatorname{LL}(1)$ Parsing Table for the given grammar:

$$
\underset{\sim}{E} \rightarrow \underset{\sim}{E}+\mathbf{T I T} ; \underset{\sim}{\mathbf{T}} \rightarrow \mathbf{T} * \mathbf{F}|\mathbf{F} ; \mathbf{F} \rightarrow(\mathrm{E})| \text { id } ;\} \mathrm{G}_{0}
$$

## - Removing Left Recursion :

$\mathrm{E} \rightarrow \mathrm{TE}{ }^{\prime}$
$\mathrm{E}^{\prime} \rightarrow+\mathrm{TE} \mathrm{E}^{\prime} \mid \epsilon$
$\mathrm{T} \rightarrow \mathrm{FT}^{\prime} \quad \mathrm{G}_{1}$
$\mathrm{T}^{\prime} \rightarrow{ }^{*} \mathrm{FT}^{\prime} \mid \in$
$F \rightarrow(E) \mid$ id

|  | First | Follow |
| :--- | :--- | :--- |
| $E$ | $c$, id | $\$)$, |
| $E^{\prime}$ | ,$+ \epsilon$ | $\$$, ) |
| T | $c$, id | ,$+ \$$, ) |
| $T^{\prime}$ | $*_{,} \epsilon$ | $+, \$)$, |
| F | $c$, id | $*_{,}+, \$$ |

* left factoring not required.
- Construction of Table : [LL (1)]

|  | $\boldsymbol{+}$ | $*$ | $\mathbf{(}$ | $\mathbf{)}$ | id | \$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| E | error | error | $\mathrm{E} \rightarrow \mathrm{TE}^{\prime}$ | error | $\mathrm{E} \rightarrow \mathrm{TE}^{\prime}$ | error |
| $\mathrm{E}^{\prime}$ | $\mathrm{E}^{\prime} \rightarrow+\mathrm{TE}$ | error | error | $\mathrm{E}^{\prime} \rightarrow \epsilon$ | Error | $\mathrm{E}^{\prime} \rightarrow \epsilon$ |
| T | error | error | $\mathrm{T} \rightarrow \mathrm{FT}^{\prime}$ | error | $\mathrm{T} \rightarrow \mathrm{FT}^{\prime}$ | error |
| $\mathrm{T}^{\prime}$ | $\mathrm{T}^{\prime} \rightarrow \epsilon$ | $\mathrm{T}^{\prime} \rightarrow * \mathrm{FT}^{\prime}$ | error | $\mathrm{T}^{\prime} \rightarrow \epsilon$ | error | $\mathrm{T}^{\prime} \rightarrow \epsilon$ |
| F | error | error | $\mathrm{F} \rightarrow(\epsilon)$ | error | $\mathrm{F} \rightarrow$ id | error |

* Since for $\mathrm{G}_{1}$, Table constructed w/o no multiple entries, hence successfully completed.

Hence $G_{1}$ is $\operatorname{LL}(1)$.
Q. Construct $\mathrm{LL}(1)$ Parsing Table for the following grammar:
$S \rightarrow L=R|R ; L \rightarrow * R| i d ; R \rightarrow L\} G_{0}$

- Left Factoring :

$$
\left.\begin{array}{l|l}
\mathbf{S} \rightarrow \mathbf{L}=\mathbf{R} \mid \mathbf{L} \\
\mathbf{L} \rightarrow * \mathbf{R} \mid \mathrm{id} \\
\mathbf{R} \rightarrow \mathbf{L}
\end{array} \Rightarrow \begin{array}{l}
\mathbf{S} \rightarrow \mathbf{L} \mathbf{X} \\
\mathbf{X} \Rightarrow=\mathbf{R} \mid \in \\
\mathbf{L} \rightarrow \text { * } \mid \mathrm{id} \\
\mathbf{R} \rightarrow \mathbf{L}
\end{array}\right\} \mathbf{G}_{1}
$$

|  | First | Follow |
| :--- | :--- | :--- |
| $\mathbf{S}$ | $*$, id | $\$$ |
| $\mathbf{X}$ | $=, \epsilon$ | $\$$ |
| $\mathbf{L}$ | $*$, id | $\$_{r}=$ |
| $\mathbf{R}$ | $*$, id | $\$,=$ |

- Construction of Table :

|  | $*$ | $=$ | id | \$ |
| :---: | :---: | :---: | :---: | :---: |
| S | $\mathrm{S} \rightarrow \mathrm{LX}$ | error | $\mathrm{S} \rightarrow \mathrm{LX}$ | error |
| L | $\mathrm{L} \rightarrow * \mathrm{R}$ | error | $\mathrm{L} \rightarrow \mathrm{id}$ | error |
| R | $\mathrm{R} \rightarrow \mathrm{L}$ | error | $\mathrm{R} \rightarrow \mathrm{L}$ | error |
| X | Error | $\mathrm{X} \rightarrow=\mathrm{R}$ | error | $\mathrm{X} \rightarrow \epsilon$ |

* $\mathrm{G}_{1}$ is a $\mathrm{LL}(1)$ Grammar.
- Hierarchy of Parsers : [for $\epsilon$-free Grammar]

* For $\epsilon$-producing grammars, every $\operatorname{LL}(1)$ may not be LALR(1).
- 

NOTE:-
We can't construct any parser for ambiguous grammar.
Except : operator precedence, parser possible for some ambiguous grammar.

* There are some unambiguous grammar, for which there are no parsers.
- Example:

1. $G: S \rightarrow a S a|b s b| a \mid b$
$L(G)=w(a+b) w R$
(odd palindrome)

- Unambiguous but no parser.
$\Rightarrow$ Every RG is not $\operatorname{LL}(1)$ as it may be ambiguous, or recursive or having common prefix.
$\Rightarrow$ Parsers exist only for the grammar if the Lang. is DCFL.
* There are some grammar whose Lang is DCFL but no parser is possible for it.
- Operation Precedence Grammar :


## Format :

1. No 2 or more variable should come side by side.
2. No $\in$ production.

- Example:

1. $\mathrm{E} \rightarrow \mathrm{E}=\mathrm{T} \mid \mathrm{T}$
$\mathrm{T} \rightarrow \mathrm{T} * \mathrm{~F} \mid \mathrm{F}$
$F \rightarrow(E) \mid$ id
O.G.
2. $E \rightarrow E+E$
$E \rightarrow E \times E$
$E \rightarrow a \mid b$
O.G.
3. $S \rightarrow A B$

$$
\begin{aligned}
& \mathrm{A} \rightarrow \mathrm{a} \mid \epsilon \\
& \mathrm{B} \rightarrow \mathrm{~b} \mathrm{~B} \mid \epsilon
\end{aligned}
$$

\{Not O.G.\}

- Checking LL(1) w/o table:
$A \rightarrow \alpha_{1}\left|\alpha_{2}\right| \alpha_{3}, \quad$ then $\rightarrow$
$\mathrm{A} \rightarrow \alpha_{1}\left|\alpha_{2}\right| \alpha_{3} \mid \in$
first $\left(\alpha_{1}\right) \cap$ first $\left(\alpha_{2}\right)=\phi$
$\operatorname{first}\left(\alpha_{1}\right) \cap$ first $\left(\alpha_{3}\right)=\phi$
$\operatorname{first}\left(\alpha_{2}\right) \cap \operatorname{first}\left(\alpha_{3}\right)=\phi$
first $\left(\alpha_{1}\right) \cap$ first $\left(\alpha_{2}\right)=\phi$
first $\left(\alpha_{1}\right) \cap$ first $\left(\alpha_{3}\right)=\phi$
first $\left(\alpha_{2}\right) \cap$ first $\left(\alpha_{3}\right)=\phi$
follow $(\mathrm{A}) \cap$ first $\left(\alpha_{1}\right)=\phi$
follow $(\mathrm{A}) \cap$ first $\left(\alpha_{2}\right)=\phi$
follow $(\mathrm{A}) \cap$ first $\left(\alpha_{1}\right)=\phi$
- BOTTOM - UP Parsers:
$\rightarrow$ It uses RMD in reverse and has no problem w/o:
(a) Left Recursion
(b) Common Prefix. $\}$
$\rightarrow$ No Parser possible for ambiguous grammar.
$\rightarrow$ There are some unambiguous grammar for which, there are no Parser.
$\rightarrow$ The Language of the grammar must be DCFL.
$L R(1)=\operatorname{LR}(0)+1$ look a head.


## - Basic Algorithm for Construction :

$\rightarrow$ Augment the grammar and expand it and give numbers to it.
$\rightarrow$ Construct LR(0) or LR(1) items.
$\rightarrow$ From these items fill the entries in the Table accordingly.

## 1. Shift Entries :

Transitions on terminals

a. $\in$ Terminal $\mathrm{I}_{0} \mathrm{I}_{1}$ : item sets.

## 2. State entry :

Transition on non-terminal (variables)

entry :

entry :


## * Shift entries are same for all

## * Same for all Bottom up Parser.

## Bottom-up Parser.

(2) Reduce Entry :

Done for each separate production in the item set of type :
$i>x \rightarrow \alpha$.

$$
\text { where }\left[\begin{array}{l}
\mathrm{i} \rightarrow \text { Prod. No } \\
\mathrm{X} \rightarrow \text { Producing var. } \\
\alpha \rightarrow \text { Grammar String. }
\end{array}\right]
$$

## In :

(a) LR(0) Parser:
Put $R_{i}$ in every cell
Of the set in action
Table
(ALL)
(b) SLR(1) Parser :

Put $\mathrm{Ri}_{\mathrm{i}}$ only in the follow( $x$ ) from the Grammar.
(Follow (x))
(c) LALR(1) and CLR(1):

Put $\mathrm{Ri}_{\mathrm{i}}$ only in the look-
ahead of the production
(Lookaheads)

- Conflicts :


## LR(0) Parser :

SR : Shift Reduce Conflict


RR: Reduce

Reduce conflict, then RR. RR


Follow (x) $\cap$ follow $(y) \neq \Phi$

- LALR(1) and CLR(1) :

Same as SLR(1), but instead $\qquad$ use the provided lookahead.

## SR


$t \in L_{2}$

RR

$L_{1} \cap L_{2} \neq \varphi$

- Inadequate Static : A static having ANY conflict is called a conflicting static or inadequate static. NOTE The static $S^{\prime} \rightarrow$. or $S^{\prime} \rightarrow S ., \$$ is excepted static, and this is not a reduction.
* The only difference $b / w \operatorname{CLR}(1)$ and $\operatorname{LALR}(1)$ is that, the states with the similar items, but different lookaheads are merged together to reduce space.

| \# state in | $=$ \#Staticin | $=$ \#Staticin | $=\leq$ \#Staticin |
| :---: | :---: | :---: | :---: |
| LR $(0)$ | SLR $(1)$ | $\operatorname{LALR}(1)$ | $\operatorname{CLR}(1)$ |

- Important Points :

1. If CLR (1) doesn't have any conflict, then conflict may or may not arise after merging in LALR(1)
2. If LALR (1) has SR-conflict, then we can conclude that CLR(1) also has SR-conflicts.
3. LALR (1) has SR-conflict if and only if CLR (1) also has SR.

* We can construct Parser for every unambiguous regular grammar [CLR (1) Parser].


| S | L | R | (1) |
| :---: | :---: | :---: | :---: |
| Simple | L to R scan | Using Rev. RMD | Lookahead |


| L | A | L | R | (1) |
| :---: | :---: | :---: | :---: | :---: |
| Look | ahead | L to R scan | Rev RMD | Lookahead |


| C | L | R | (1) |
| :---: | :---: | :---: | :---: |
| Canonical | L to R Scan | Rev. RMD | Lookahead |

- Very Important Point :

LALR (1) Parser can parse non LALR (1) grammar which only has SR-conflict by favouring shift over reduce.
Eg.
$\mathrm{E} \rightarrow \mathrm{E}+\mathrm{E}|\mathrm{E} * \mathrm{E}|$ id $\mid 2+3 * 5 \Rightarrow \mathrm{E}+\mathrm{E} . * 5$

- CD - Lexical Analysis

| Char. Stream <br> $\downarrow$ |  |  |
| :---: | :--- | :--- |
| Lexical .A. <br> Token Stream | Token Generators <br> Scanner | defn: Scan the whole <br> program, char. by char |
|  | Linear Phase <br> and producer the |  |
|  | Token Recognixer | corresponding token. |

* Also produce/reports the text Lexical Errors (if any)
- Functions of Lexical Analyzer:
i) Scans all the characters of the program.
ii) Token Recognizer.
iii) Ignores the comment \& spaces
iv) Maximal Matching Rule [Longest prefix match].
- NOTE:

The Lexical analyser uses, the Regular Expression.

- Prioritization of Rules.
- Longest Prefix match

Lexeme $\rightarrow$ Smallest unit of program or Logic

Lexmes

Token $\rightarrow$ Internal representation of Lexeme. LA
Tokens

## Types of Token:

1. Identifier
2. Keywords
3. Operators
4. Literals/constants
5. Special symbol

## Token Separation:

1. Spaces
2. Punctuation

## Implementation:

$\rightarrow$ LEX tool $\Rightarrow$ Lex. yy. C

* All identifier will have entry in symbol Table, LA, gives entries into the symbol Table.
[Regular Expression $\rightarrow$ DPA $\rightarrow$ Lexical Analyzer]
- Find no. of Tokens :

1. void main ( )
\{ printf ("gate");
[10 Tokens]
2. int x , * P ;

X = 10;
$\mathrm{P}=$ \& x ;
x + +;
[18 tokens]
3. int x ;
$x=y$;
$\mathrm{x}=\mathrm{=} \mathrm{y}$;
[11 Tokens]
4. int $1 \times 2,3$;
[Lexical Error]
5. Char ch = 'A' ;
[5 Token]
6. char ch = 'A ;

Lexical Error
7. char * $\mathrm{P}=$ "gate";
[6 Tokens]
8. char * $\mathrm{P}=$ "gate";
[Error]
9. int $x=10$;
/* comment
$x=x+1 ;$
Error
10. int $x=10$;

Comment * /
$x=x+1 ;$
[14 Tokens]

- CD - Syntax Directed Translation

CFG + Translation
SDT :
CFG + Translation
$\Rightarrow$ Syntax + Translation


- Example:
$S \rightarrow S_{1} S_{2}$ [S. count $=S_{1}$ count $+S_{2}$ count]
$S \rightarrow\left(S_{1}\right)$ [S. count $=S_{1}$ count +1 ]
$S \rightarrow \in[S$. count $=0]$
* Count is an attribute for non-terminal.
- Application of SDT :

1. Used to perform Semantic Analysis
2. Produce Parse Tree
3. Produce intermediate Rep.
4. Evaluate an expression
5. Convert infix to prefix or postfix.

## - Attributes :

1. Inherited Attribute
2. Synthesized Attribute


- Inherited Attribute : (RHS)
$\mathbf{S} \rightarrow \mathbf{A}$ B $\{A . x=f(B . x \mid S . x)\}$
The computation at any node (non-terminal) depends on parent or sibling(s).
* In Above example $x$ is inherited attribute.
- Synthesized Attribute : (LMS)
$\underset{S}{\rightarrow} \rightarrow \mathbf{A}$ B $\{S . x=f(A . x \mid B . x\}$
x is synthesized attribute.
The computation of any node (non-terminal) depends on children.
- Identifying Attribute Type :
* Always check every Translation.

1. 

$$
\begin{aligned}
& \mathrm{D} \rightarrow \mathrm{~T}: \mathrm{L} \text {; \{L. Type = } \mathrm{T} . \text { Type }\} \text { inherited. } \\
& \mathrm{L} \rightarrow \text { id }
\end{aligned}
$$

Type in neither inherited nor syntesized.
2.


Val is synthesized attribute.
3.
$S \rightarrow A B\{A a=B \cdot x ; S . y=A . x\} x$ is inherited $\mid y$ is synth $A \rightarrow a\{A, y=a\} y$ is synth $B \rightarrow b\{B . y=a . y\} y$ is synth
$\mathbf{x} \Rightarrow$ Inherited
$y \Rightarrow$ Synthesized
4.
$D \rightarrow$ (L) $\{\mathrm{L}$. in $=\mathrm{T}$. type $\}$ inherited(in)
$T \rightarrow$ int $\{$ T. type ] int $\}$ synth (type).
L $\rightarrow$ id \{Add Type (id. entry, L. in)\}
in $\Rightarrow$ Inherited
type $\Rightarrow$ Synthesized

- Syntax Directed Definitions (SDDs) : (Attribute Grammar)

1. L-Attributed Grammar :
$\rightarrow$ Attribute is synthesized or restricted inherited.

$\rightarrow$ Translation can be appended any where is RHS of production.
2. S-attributed Grammar :
$\rightarrow$ Attribute is synthesized only
$\rightarrow$ The translation is placed only at the end of production.

$$
\begin{array}{ll}
S \rightarrow A V\{A . x=S . x+2\} & \text { Eg. } S \rightarrow A B\{S . x=f(A x \mid B x)\} \\
\text { or, } S \rightarrow A B\{B . x=f(A . x \mid S . x)\} & \rightarrow \text { Evaluation : Rev. RMD (Bottom up Parsing) } \\
\text { or, } S \rightarrow A B\{S . x=f(A . x \mid B . x)\} & L-\text { Attri. } \\
\text { S - Attri. }
\end{array}
$$

- Identify SDD :

(E) $\rightarrow$ id
$\{\mathrm{E}$. type $=$ lookup (id .entry) $\}$ else type error. Synth.
$\therefore$ type is synthesized, hence S-Attribute and also L-attributed Grammar.
* Every S-attributed Grammar is also L-attributed Grammar.
* For L-attributed Evaluation, use the In-order of annotated Pares Tree.
* For S-attributed, Reverse of RMD is used.
$\rightarrow$ Find RMD order
$\rightarrow$ Consider in Reverse
- CD- Intermediate Representation

- Example expression : $(y+z) *(y+z)$

$$
\begin{aligned}
& \text { Postfix } \rightarrow y z+y z+* \\
& 3 A C \rightarrow \begin{array}{l}
t_{1}=y+z \\
t_{2}=t_{1} * t_{1}
\end{array}
\end{aligned}
$$

Syntax Tree $\rightarrow$


## DAG $\rightarrow$ <br>  <br> Reverse the atready existing common sub expression.

- 3-Address Code : Code in which, at most 3 addresses.
[including LHS]



| 0 | * | z | y |
| :---: | :---: | :---: | :---: |
| 1 | + | y | (0) |
| 2 | - | (1) | a |
| 3 | $=$ | (2) |  |


| 0 | $\mathbf{x}$ | z | y | $\mathrm{t}_{1}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | + | y | $\mathrm{t}_{1}$ | $\mathrm{t}_{2}$ |
| 2 | - | $\mathrm{t}_{2}$ | a | $\mathrm{t}_{3}$ |
| 3 | $=$ | $\mathrm{t}_{1}$ |  | x |


|  | $(0)$ |
| :--- | :--- |
|  | $(1)$ |
| 8 | $(2)$ |
|  | $(3)$ |

$\rightarrow$ Indirect Notation pointers to the rows of Triple.

## Triple Notation

$\rightarrow$ Space efficient
$\rightarrow$ time in inefficient

* 3AC done using operator precedence.
- Find min no of variable reqd. in equivalent 3 AC :


$\therefore$ Minimum :
$\left\{\begin{array}{l}\mathrm{b}=\mathrm{b}+\mathrm{b} \\ \mathrm{c}=\mathrm{b}+\mathrm{c} \\ \mathrm{a}=\mathrm{c}+\mathrm{d}\end{array}\right\} \Rightarrow \begin{aligned} & \text { only } 3 \text { variable } \\ & {[\text { Most optimal] }}\end{aligned}$
- Static Single Assignment code (SSA code) :

Every variable (addr) in the code has single assignment.
[Single meaning] + 3 AC.
(1)

(2)


- Control flow Graphs :

Basic Blocks: Seq. of 3-addr code, which control entire from $1^{\text {st }}$ stmt and exists from last.

* Basic blocks can never contain jump statement in b/w.

Find Leaders to identify basic blocks.
$\rightarrow 1^{\text {st }} 3 \mathrm{AC}$ is leader
$\rightarrow$ Target of Jumps are Leader
$\rightarrow$ Statement Just below Jump are Leaders
$\rightarrow$ Jump is itself a Leader.

- Example:

1. $i=1-L \quad B_{1}$
2. $\mathbf{j = 1}-\mathbf{L} \mathbf{B}_{2}$
3. $\mathbf{t}_{1}=\mathbf{t} * \mathbf{i}-\mathbf{L} \quad B_{3}$
4. $\mathbf{t}_{2}=\mathbf{t}_{1}+\mathbf{5}$
5. $t_{3}=4 * t_{2}$
6. $\mathbf{t}_{4}=\mathbf{t}_{3}$
7. $a\left[t_{4}\right]=1$
8. $\mathbf{j}=\mathbf{j}+1$
9. 


10.

$$
i=i+1-L B_{5}
$$

11. if $\mathrm{i}<\mathbf{5}$ goto $2-L B_{6}$


- CD - Code Optimization
$\rightarrow$ Saves space/time. (Basic Objective)

- Optimization Methods :

1. Constant folding
2. Copy propagation
3. Strength reduction
4. Dead code elimination
5. Common sub expr elimination
6. Loop optimization


## 1. Constant Folding :



Folding

## 2. Copy Propagation :

i) Variable propagation :
$x=y ;$
$z=x+2 ; \quad z \quad z=y+2 ;$
$\mathbf{x}=\mathbf{2 + y * 3 ]}$ Can't fold the constants.
ii) Constant propagation :
$x=3$
$z=x+a ; \Rightarrow z=3+a ;$
3. Strength Reduction :

Replace expensive statement/instruction with cheaper one.

$x=y / \delta ; \Rightarrow x=y \gg 3 ;$
4. Dead code Elimination :


* Hence, its a code, that never execute, during execution. We can always delete such code.

5. Common Subexpression elimination

DAT is used to eliminate common sub expression.
Eg. $x=(\underline{a+b})+(\underline{a+b})+c ; \Rightarrow \quad t_{1}=a+b$

$$
x=t_{1}+t_{1}+c
$$



6. Loop Optimization :
(i) Code Motion - Freq Reduction :

Move the loop invariant code outside of Loop.

$$
\begin{aligned}
& x=10 ; \\
& y=y+i ;
\end{aligned}
$$

$$
\text { for }(i=0 ; i<n ; i++)\}
$$

x = 10;

$$
\}
$$

(ii) Induction Variable elimination :
$\mathrm{i}_{1}=\mathbf{0}$;
$\mathrm{i}_{2}=\mathbf{0}$;
for ( $\mathbf{i}=\mathbf{0} \mathbf{;} \mathbf{i}<\mathbf{n} \mathbf{i} \mathbf{i}+\boldsymbol{+}$ ) $\{$
$A\left[\mathbf{i}_{1}++\right]=\mathbf{B}\left[\mathbf{i}_{2}++\right] ;$
\}

## $\mathrm{i}, \mathrm{i}_{1}, \mathrm{i}_{2}: \mathbf{3}$ induction variables

$\Rightarrow \quad A[i]=B[i] ;$
for ( $\mathbf{i}=\mathbf{0} \boldsymbol{i} \mathbf{i}<\mathbf{n} \boldsymbol{i} \mathbf{i + +}$ ) $\{$ \}

Only 1 induction variable: i
(iii) Loop Merging/combining : (Loop Jamming)

| $3 \mathrm{n}+2$ | for ( $\mathbf{i}=\mathbf{0} \mathbf{i} \mathbf{i}<\mathbf{n} \mathbf{i} \mathbf{i + +}$ ) | for ( $\mathrm{i}=\mathbf{0} \mathbf{i} \mathbf{i}<\mathbf{n} \mathbf{i} \mathbf{i + +}$ ) $\boldsymbol{f}$ |
| :---: | :---: | :---: |
| 3n + 2 | $A[i]=i+1 ;$ | $A[i]=i+1$ |
| $6 \mathrm{n}+4$ | B [j] = j + 1; |  |

(iv) Loop cooling:
(1)

$$
\text { for }(i=0 ; i<3 ; i++) \quad \Rightarrow
$$

print f ("CD");
$3 \times 3+2=11$ Statements

Print f("CD");
Print f("CD");
3 statements
(2)
for ( $\mathrm{i}=0 ; \mathrm{i}<2 \mathrm{n} ; \mathrm{i}++$ ) \{ $\Rightarrow$ print f("CD");
\{
$(2 \times 3 n+2)=6 n+2$

Reduced


[^0]:    * Parsers are basically DPDA's.

