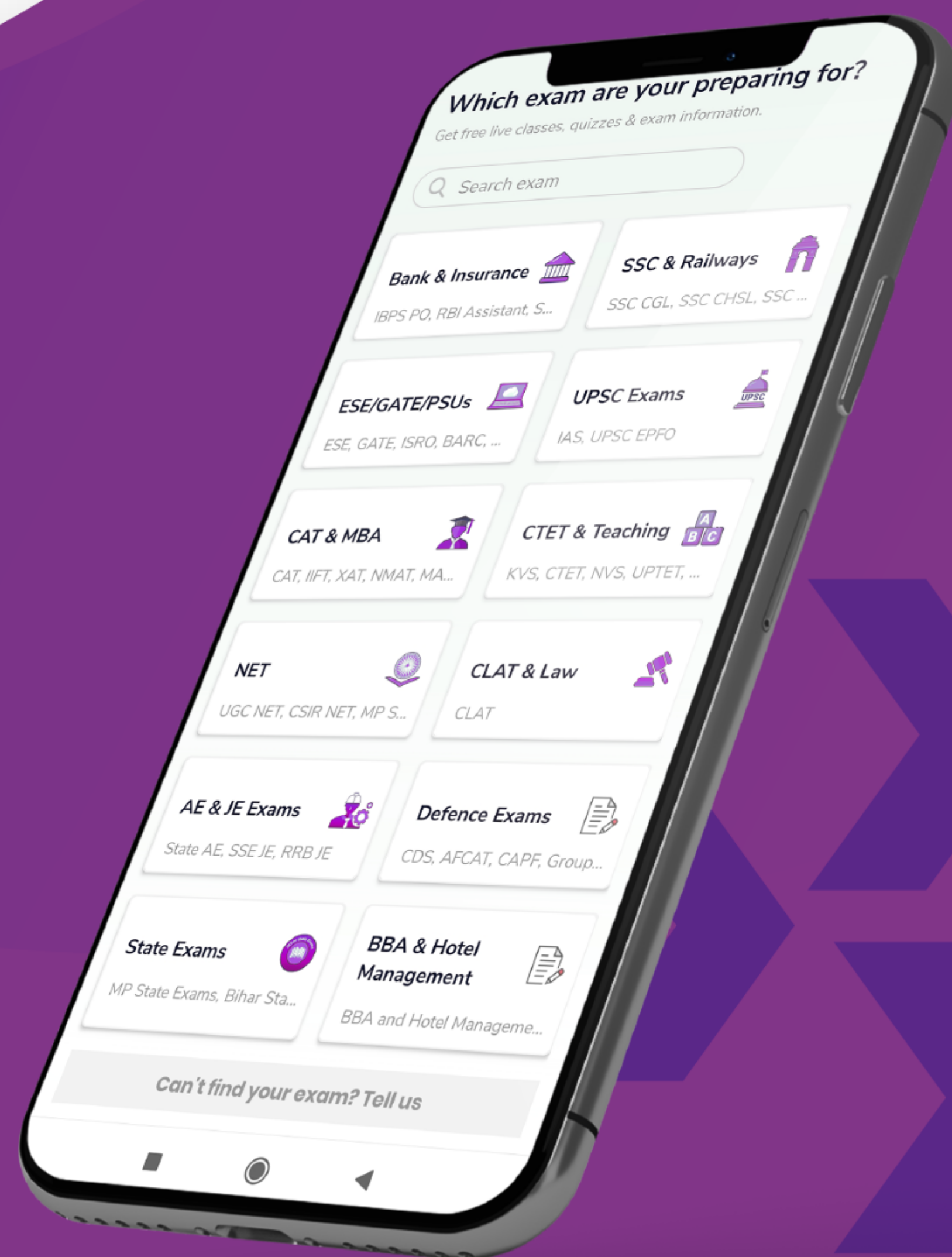


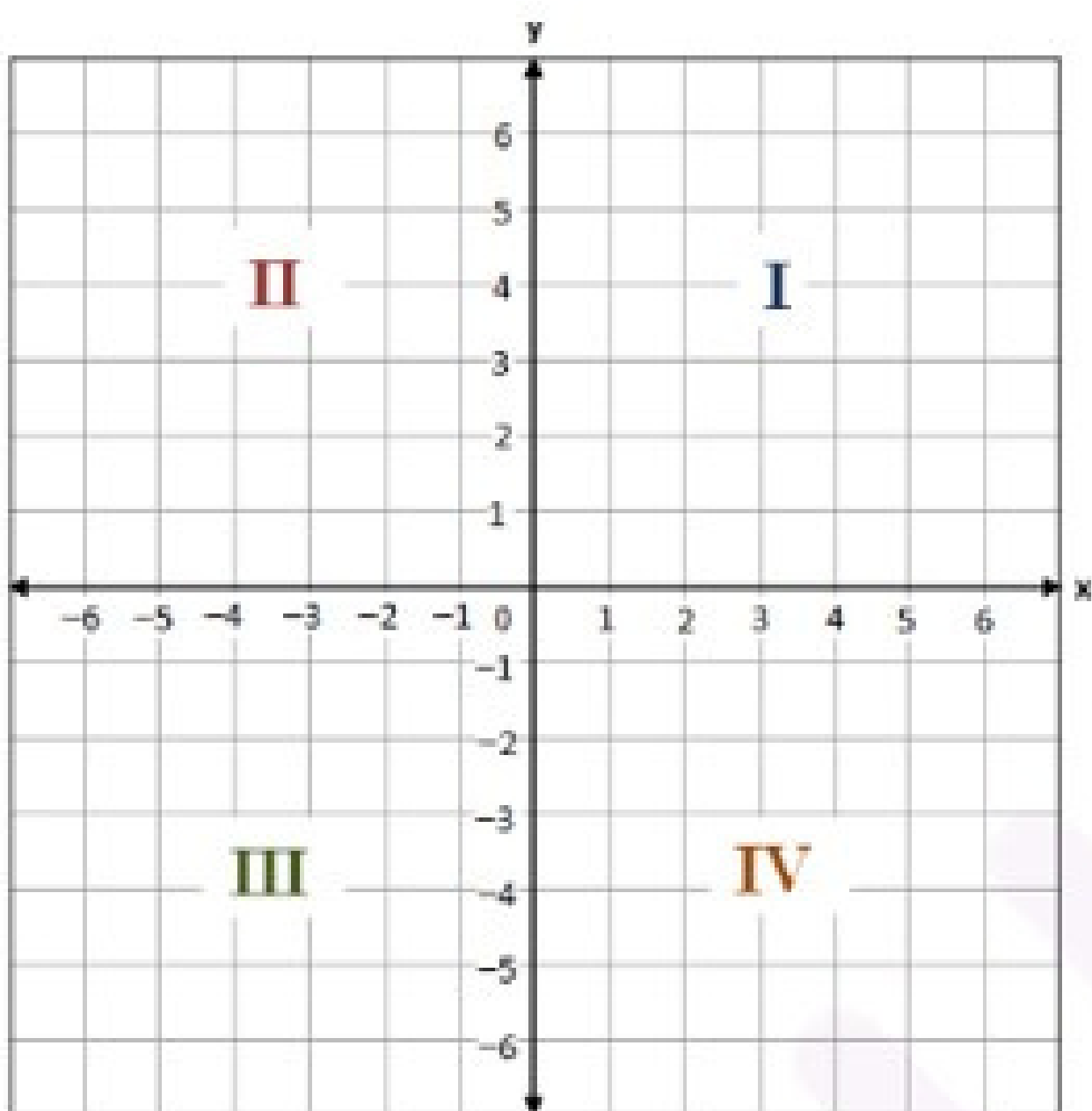
# Formula Sheet On Coordinate Geometry



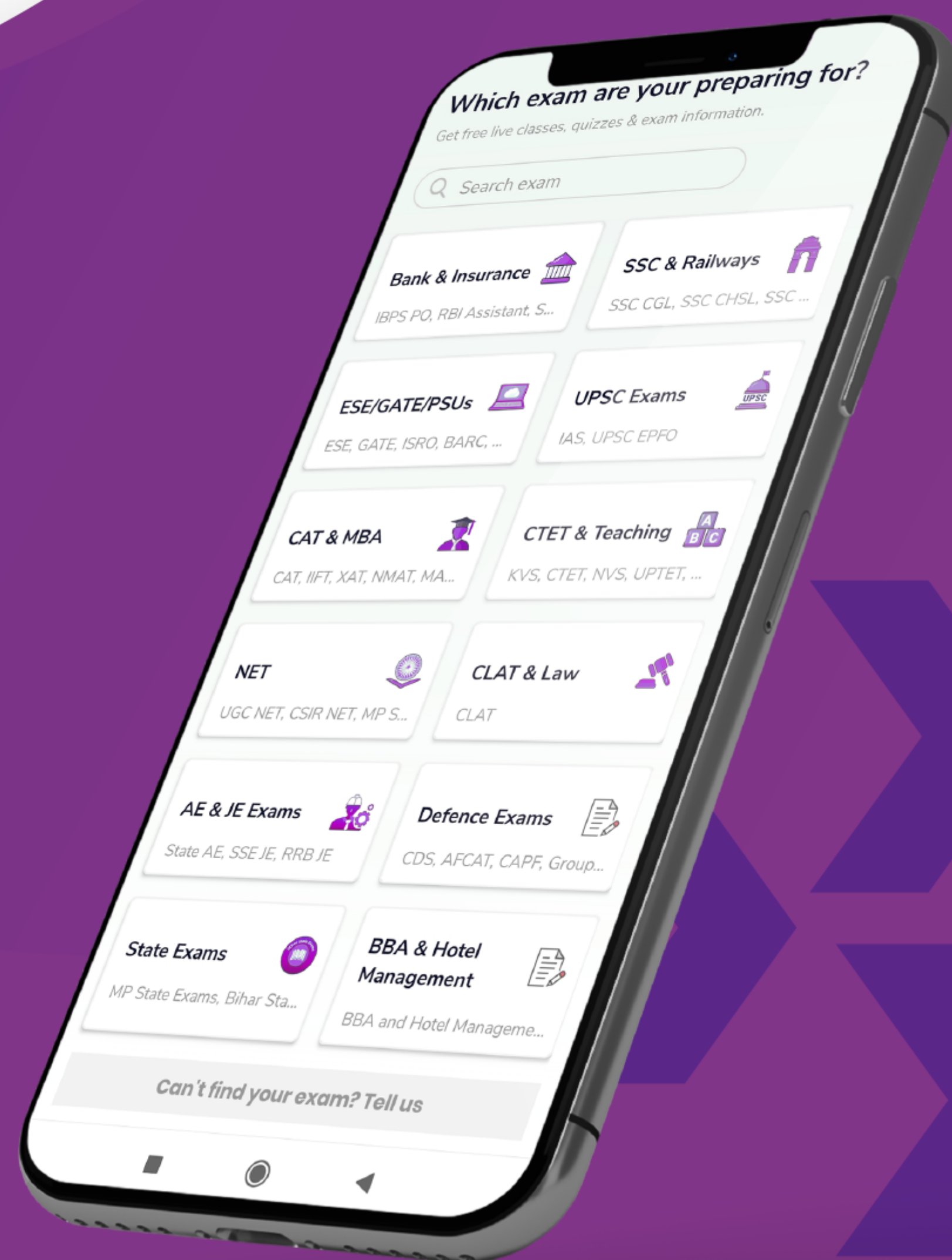


## Defination

**Co-ordinate Plane:** A coordinate plane is a 2-D plane formed by the intersection of a vertical line called y-axis and a horizontal line called x-axis. These are perpendicular lines that intersect each other at zero, and this point is called the origin O (0, 0). The axes cut the coordinate plane into four equal sections, and each section is known as quadrant.



The two-dimensional plane is called the Cartesian plane, or the coordinate plane and the axes are called the coordinate axes or x-axis and y-axis. The given plane has four equal divisions by origin called quadrants.



## Important Points

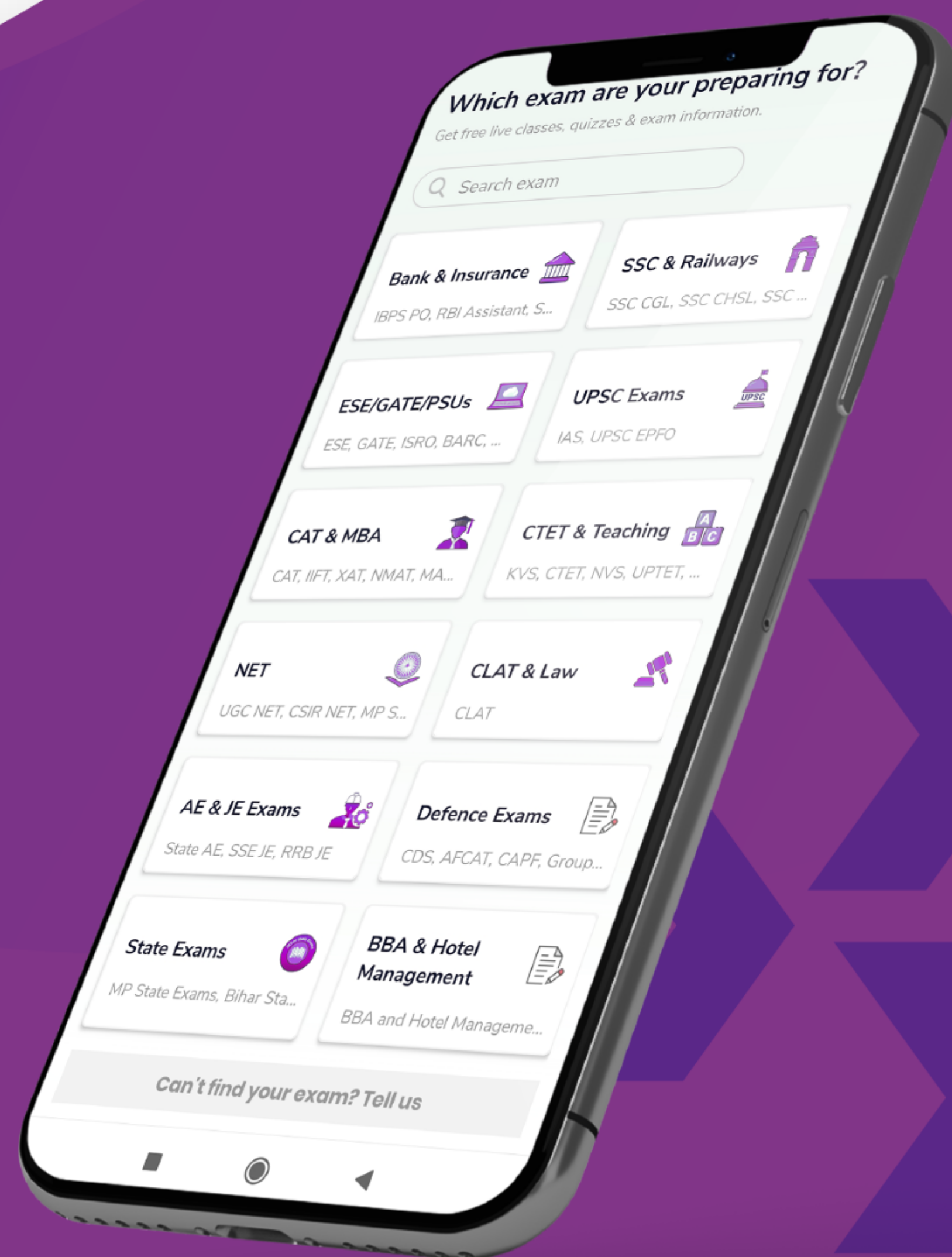
The two-dimensional plane is called the Cartesian plane, or the coordinate plane and the axes are called the coordinate axes or x-axis and y-axis. The given plane has four equal divisions by origin called quadrants.

- The horizontal line towards the right of the origin (denoted by O) is positive x-axis.
- The horizontal line towards the left of the origin is negative x-axis.
- The vertical line above the origin is positive y-axis.
- The vertical line below the origin is negative y-axis.
- The x-coordinate or abscissa of a point is its perpendicular distance from the y-axis measured along the x-axis.
- The y-coordinate or ordinate of a point is its perpendicular distance from the x-axis measured along the y-axis.
- In stating the coordinates of a point in the coordinate plane, the x-coordinate comes first, and then comes the y-coordinate. We place the coordinates in brackets as (x, y). Distance between two points  $(x_1, y_1)$ ,  $(x_2, y_2)$ :



$$\text{Distance} = AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$





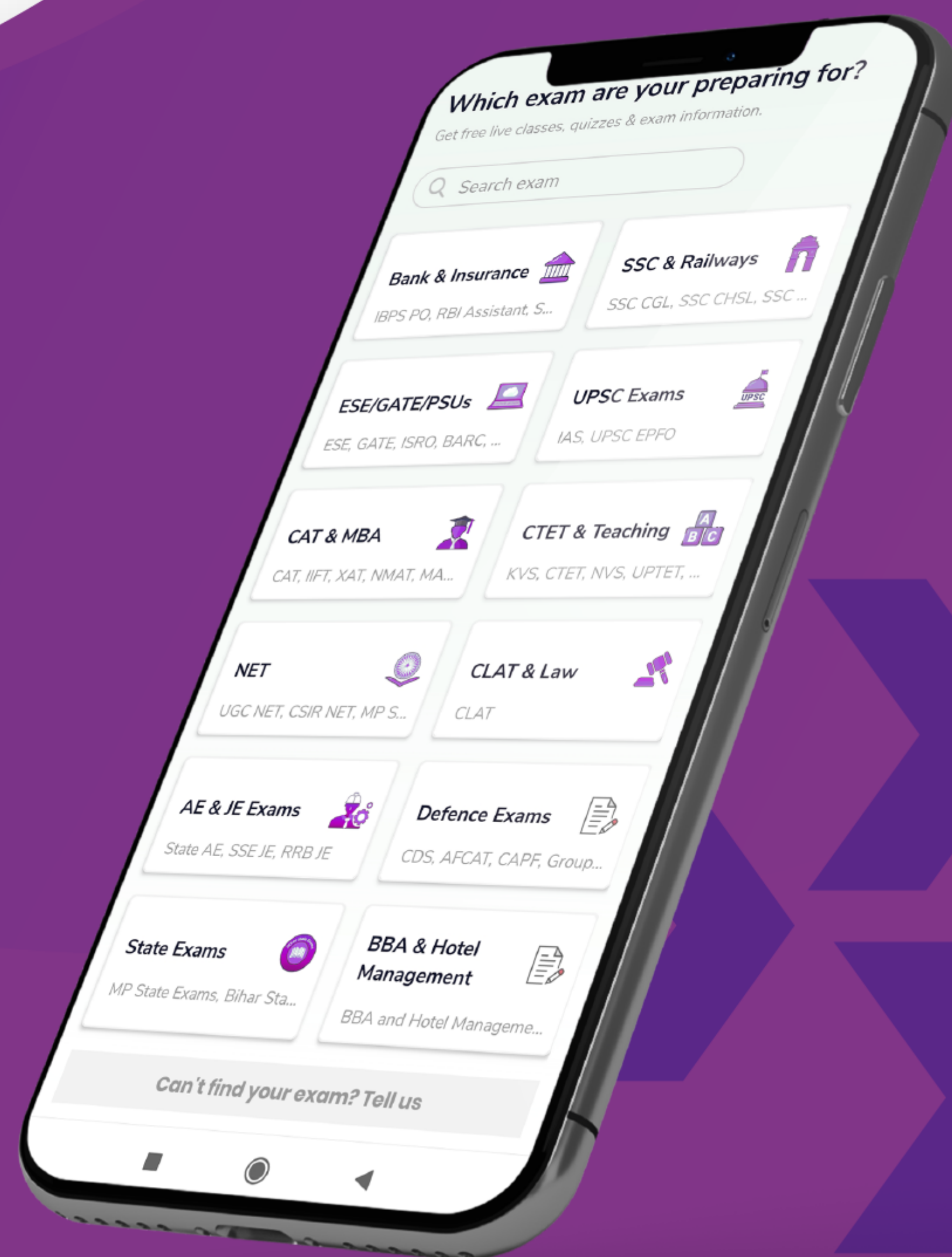
## Section Formula:

**Section Formula:** The co-ordinates of a point  $P(x, y)$ , dividing the line segment joining the two points  $A(x_1, y_1)$  and  $B(x_2, y_2)$  internally in the ratio  $m : n$  are given by

$$x = \frac{m \cdot x_2 + n \cdot x_1}{m + n}, y = \frac{m \cdot y_2 + n \cdot y_1}{m + n}$$

The co-ordinate of the point  $P(x, y)$ , dividing the line segment joining the two points  $A(x_1, y_1)$  and  $B(x_2, y_2)$  externally in the ratio  $m : n$  are given by

$$x = \frac{m \cdot x_2 - n \cdot x_1}{m - n}, y = \frac{m \cdot y_2 - n \cdot y_1}{m - n}$$



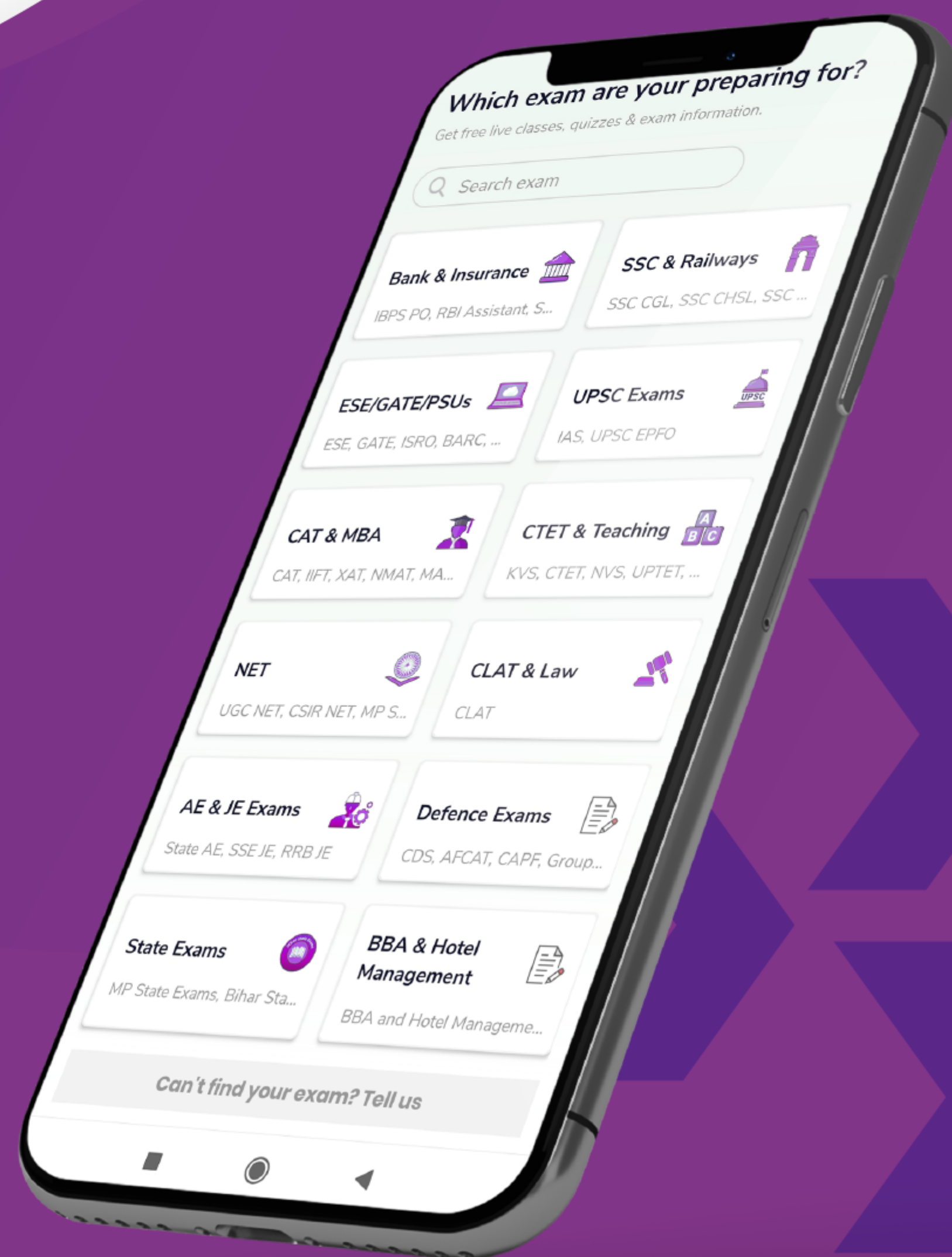
## Trisection Formula of a line segment:

**Trisection Formula of a line segment:** If points P and Q which lie on line segment AB divide it into three equal parts that means, if  $AP = PQ = QB$  then the points P and Q are called Points of Trisection of AB



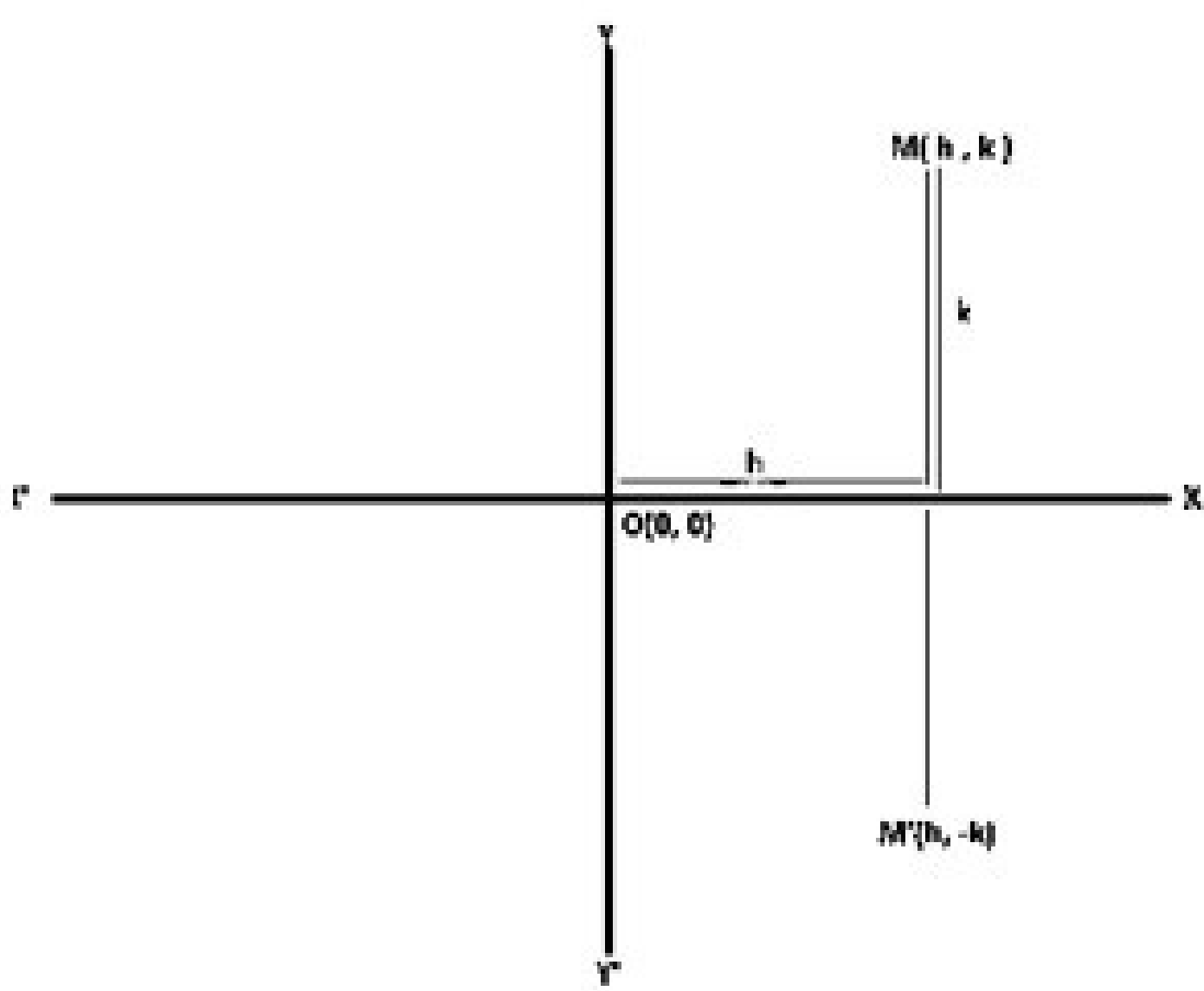
Here, P divides AB in the ratio 2 : 1 and Q divides AB in the ratio 1 : 2. Now use the section formula for finding the coordinates of P and Q.





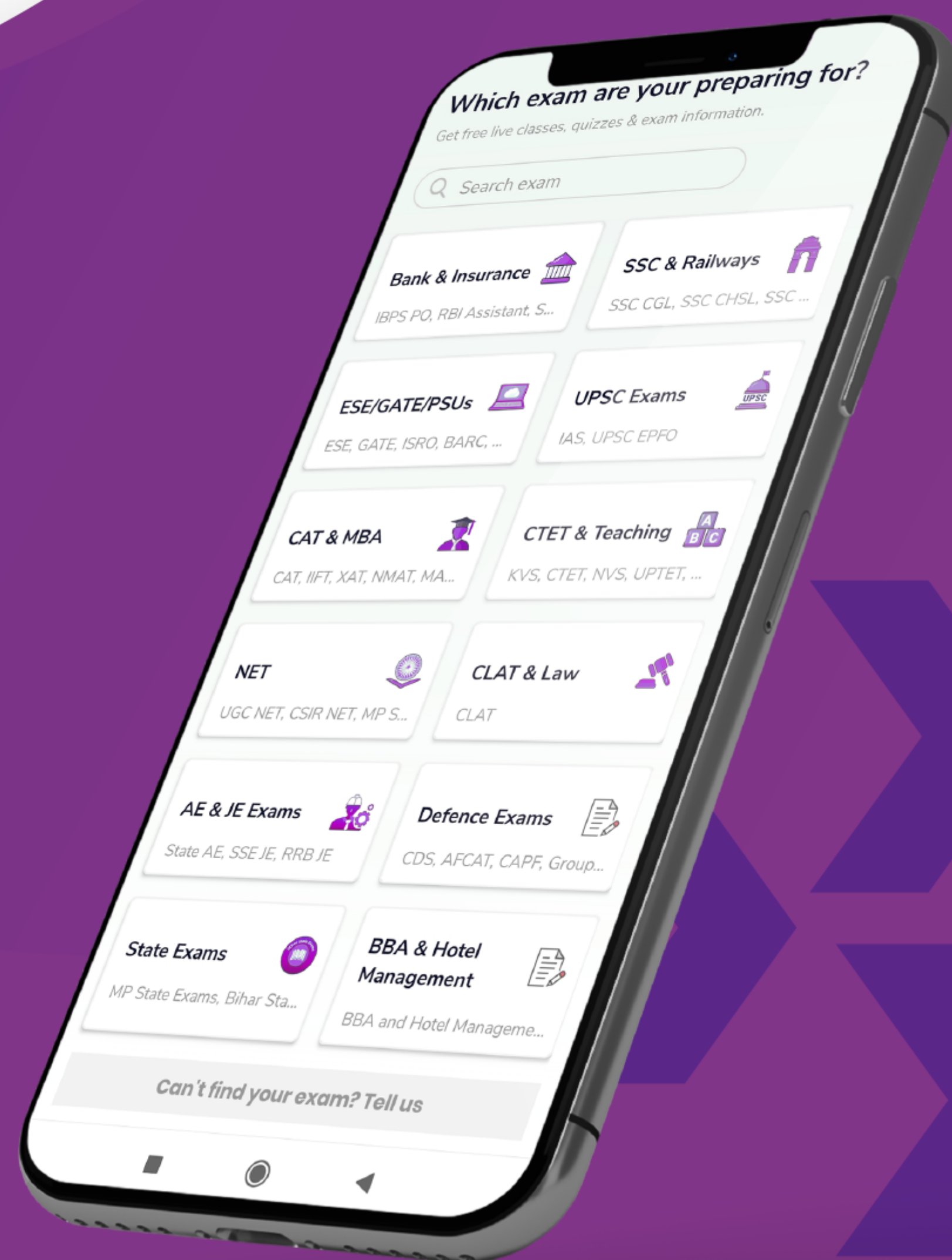
## Reflection in the X-axis:

1. Reflection in the X-axis: Here, x-axis represents the plain mirror. When point M is reflected in x-axis, the image M' is formed in the horizontally opposite quadrant whose co-ordinates are (h, -k). Thus, when a point is reflected in x-axis, then the x-co-ordinate remains same, but the y co-ordinate becomes negative



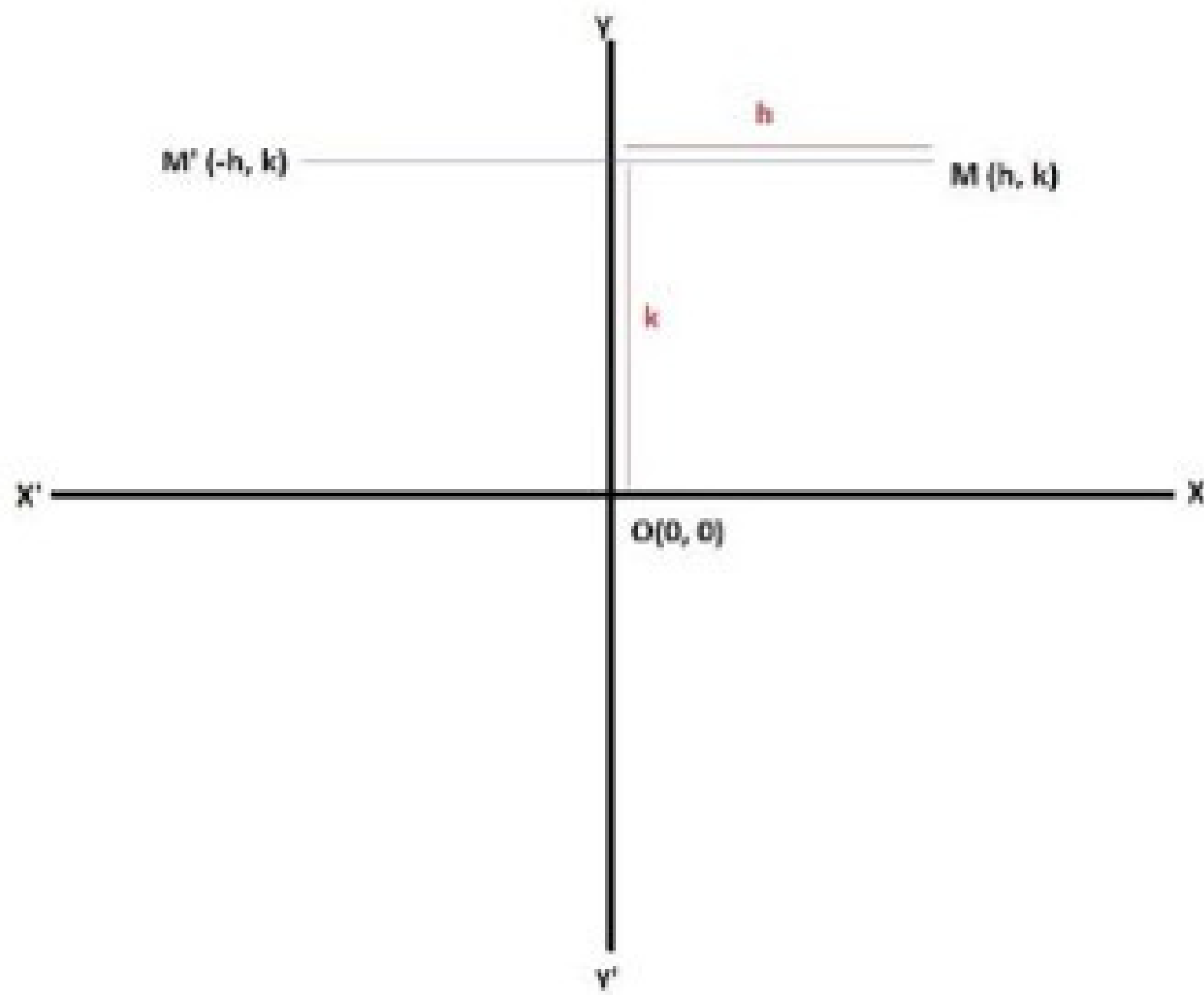
Thus, the image of point M (h, k) is M'(h, -k). Rule:

- (i) Retain the abscissa i.e., x-coordinate.
- (ii) Change the sign of ordinate i.e., y-coordinate.



## Reflection in the Y-axis

2. Reflection in the Y-axis: Here, y-axis represents the plane mirror. when point M is reflected in y-axis, the image M' is formed in the vertically opposite quadrant whose co-ordinates are  $(-h, k)$ . Thus, when a point is reflected in y-axis, then the y-co-ordinate remains same and then x-co-ordinate become negative.



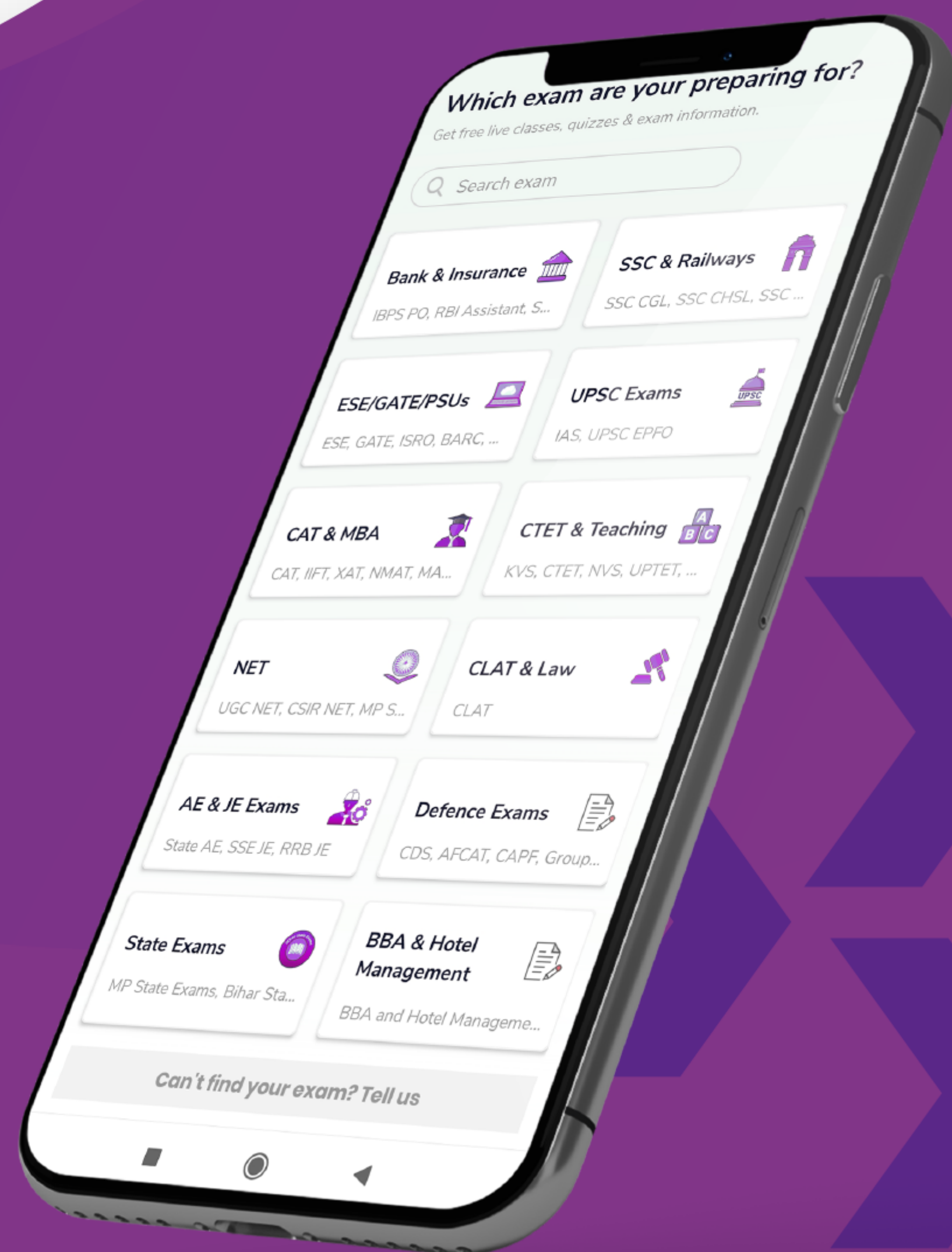
Thus, the image of  $M(h, k)$  is  $M'(-h, k)$ .

### Rule:

(i) Change the sign of abscissa i.e., x-coordinate.

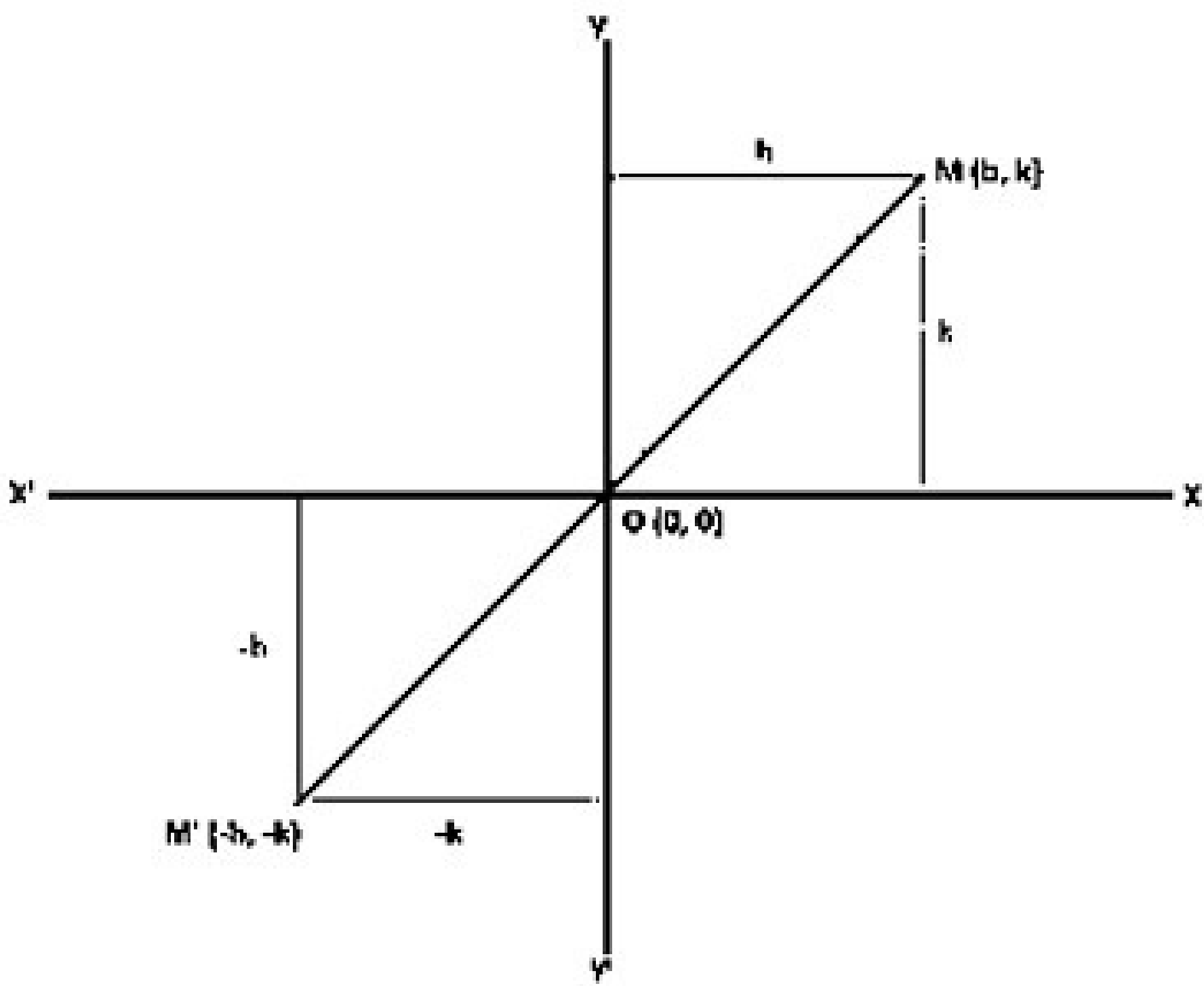
(ii) Retain the ordinate i.e., y-coordinate.





## Reflection through Origin:

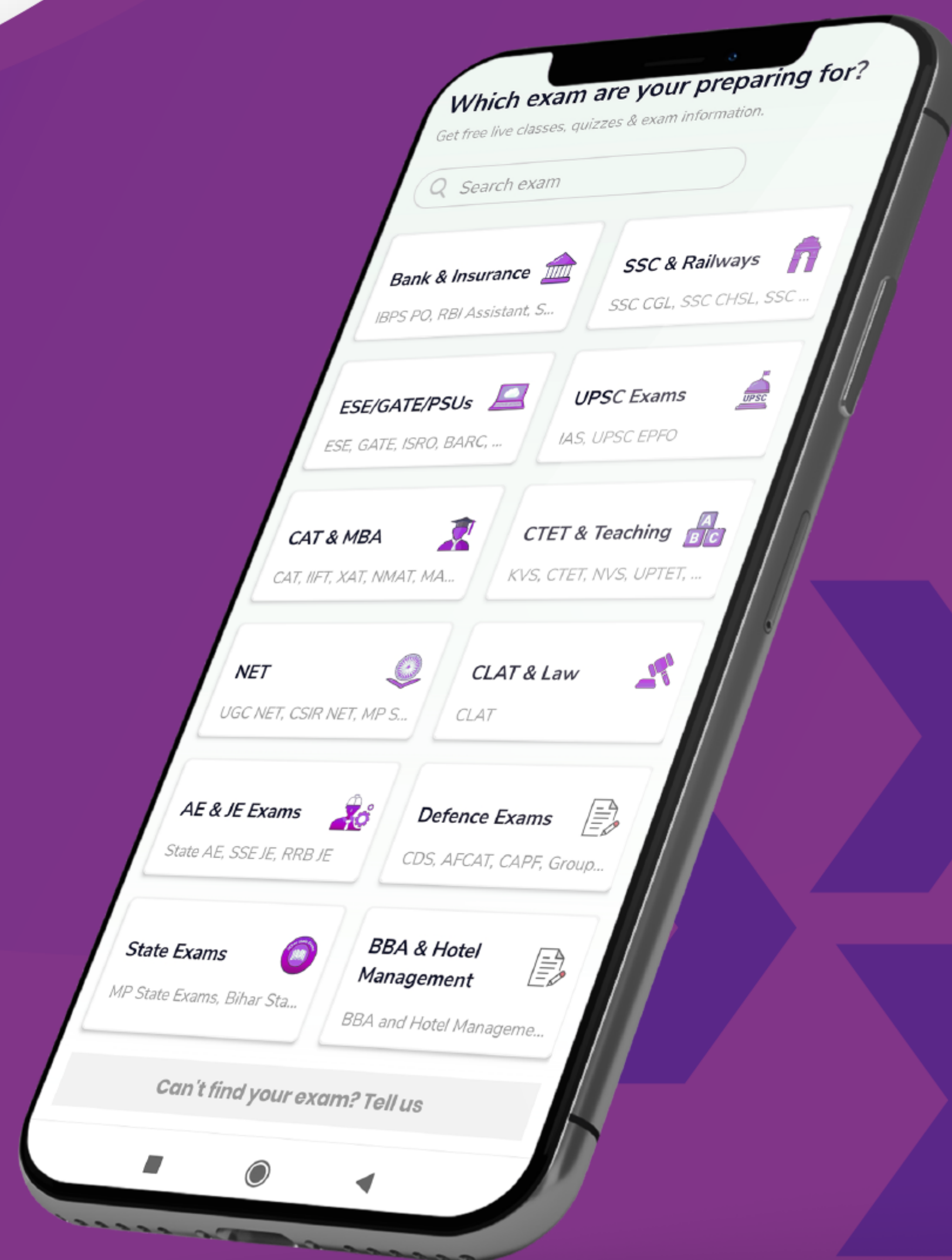
3. Reflection through Origin: When a point is reflected in origin, both x-co-ordinate and y-co-ordinate change. Thus, the reflection of  $M(h, k)$  is  $M'(-h, -k)$  in the origin.



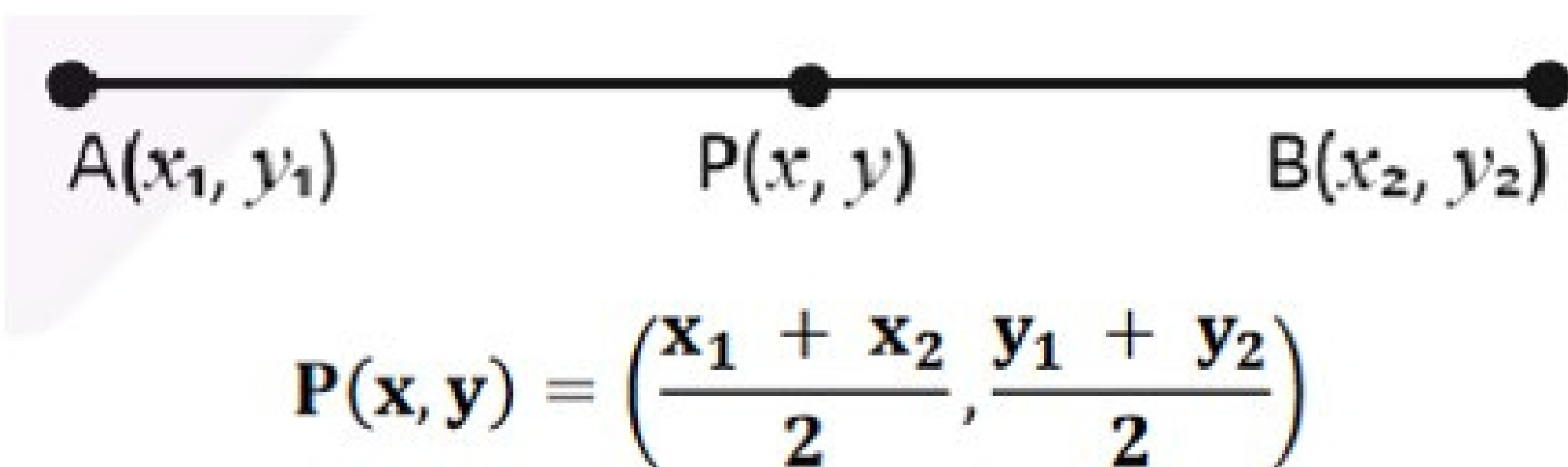
Rule:

- (i) Change the sign of abscissa i.e., x-coordinate.
- (ii) Change the sign of ordinate i.e., y-coordinate.

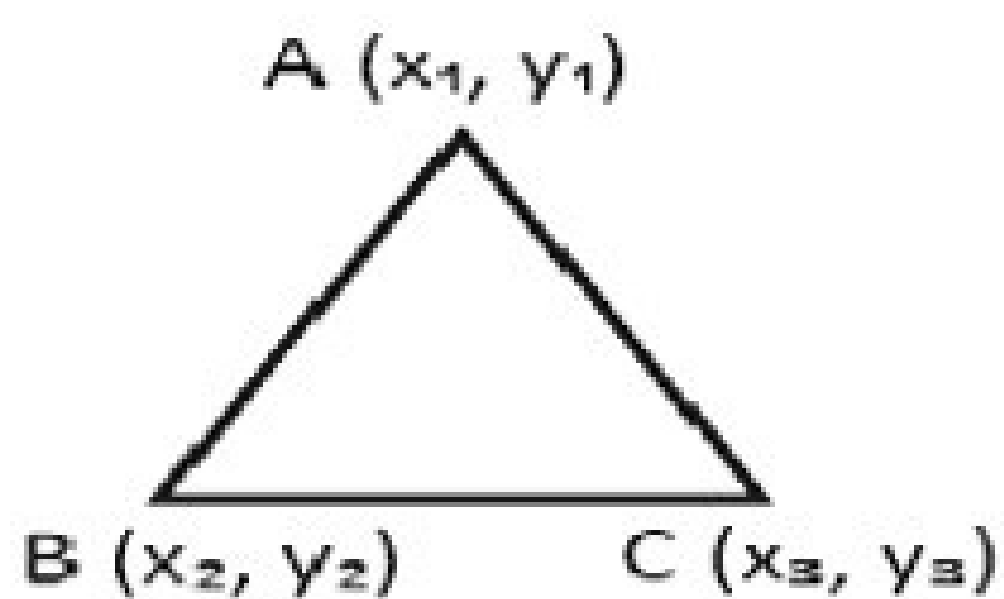




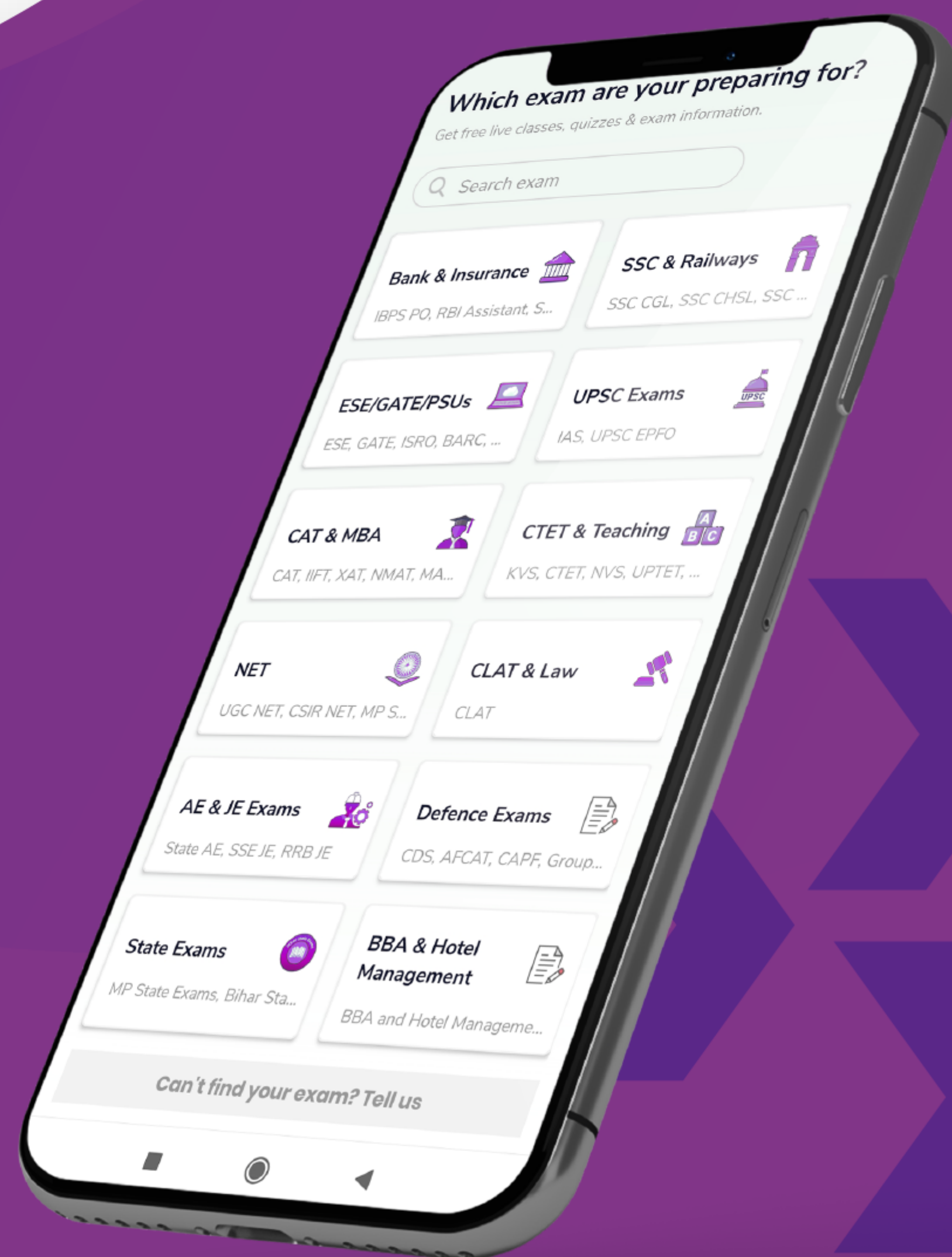
The co-ordinates of midpoint of the line formed by  $A(x_1, y_1)$ ,  $B(x_2, y_2)$ : Here, P point divides the line segment AB into ratio 1:1. Thus,  $m = n = 1$ .



Area of triangle whose coordinates are  $A(x_1, y_1)$ ,  $B(x_2, y_2)$ ,  $C(x_3, y_3)$ :



Area of the Triangle ABC  $\frac{1}{2} |x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)|$



## Collinear Points

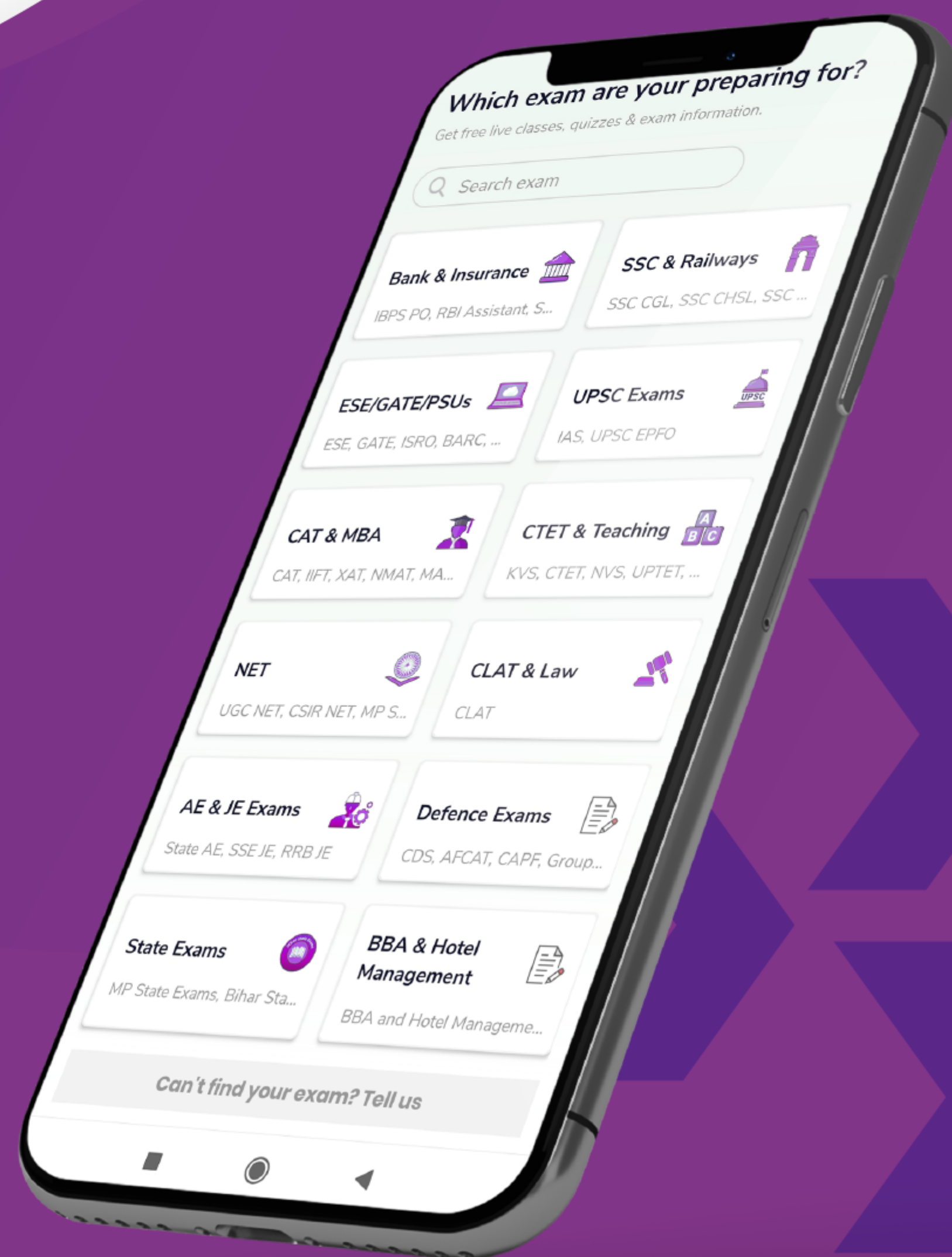
**Collinear points:** Three or more points that lie on a same straight line are called collinear points. There are two methods to find if three points are collinear:

(i) Slope formula method: Three or more points are collinear, if slope of any two pairs of points is same. Let three points be A, B and C, three pairs of points can be formed as AB, BC and AC.

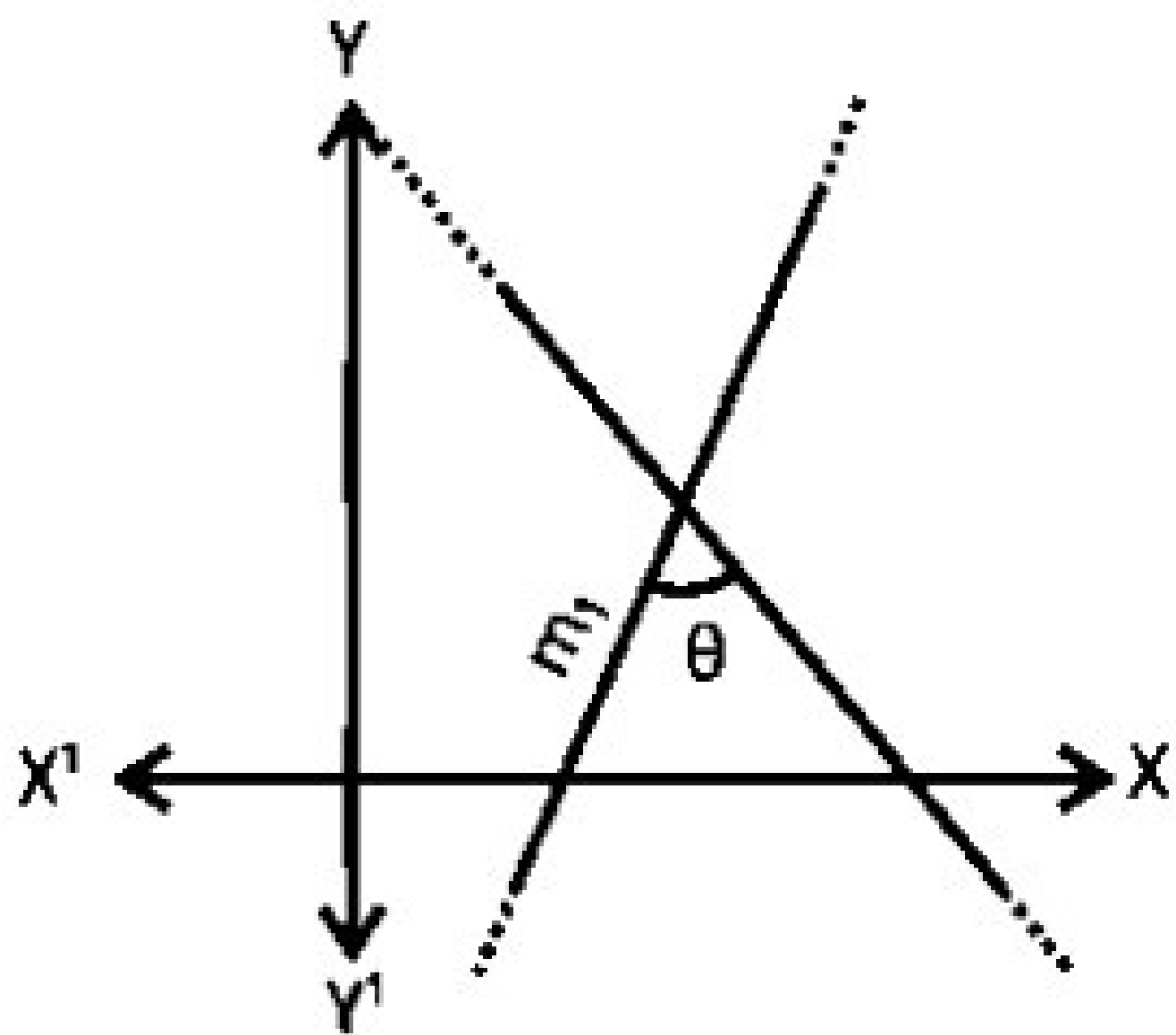
If slope of AB = slope of BC = slope of AC, then A, B and C are collinear points. (ii) Area of triangle method: Three points are collinear if the value of area of triangle formed by the three points is zero. Slope of a line: If a line joining two points  $A(x_1, y_1)$  and  $B(x_2, y_2)$  then the slope of the line joining the two points.

$$m = \frac{y_2 - y_1}{x_2 - x_1} = -\frac{\text{coefficient of } x}{\text{coefficient of } y}$$



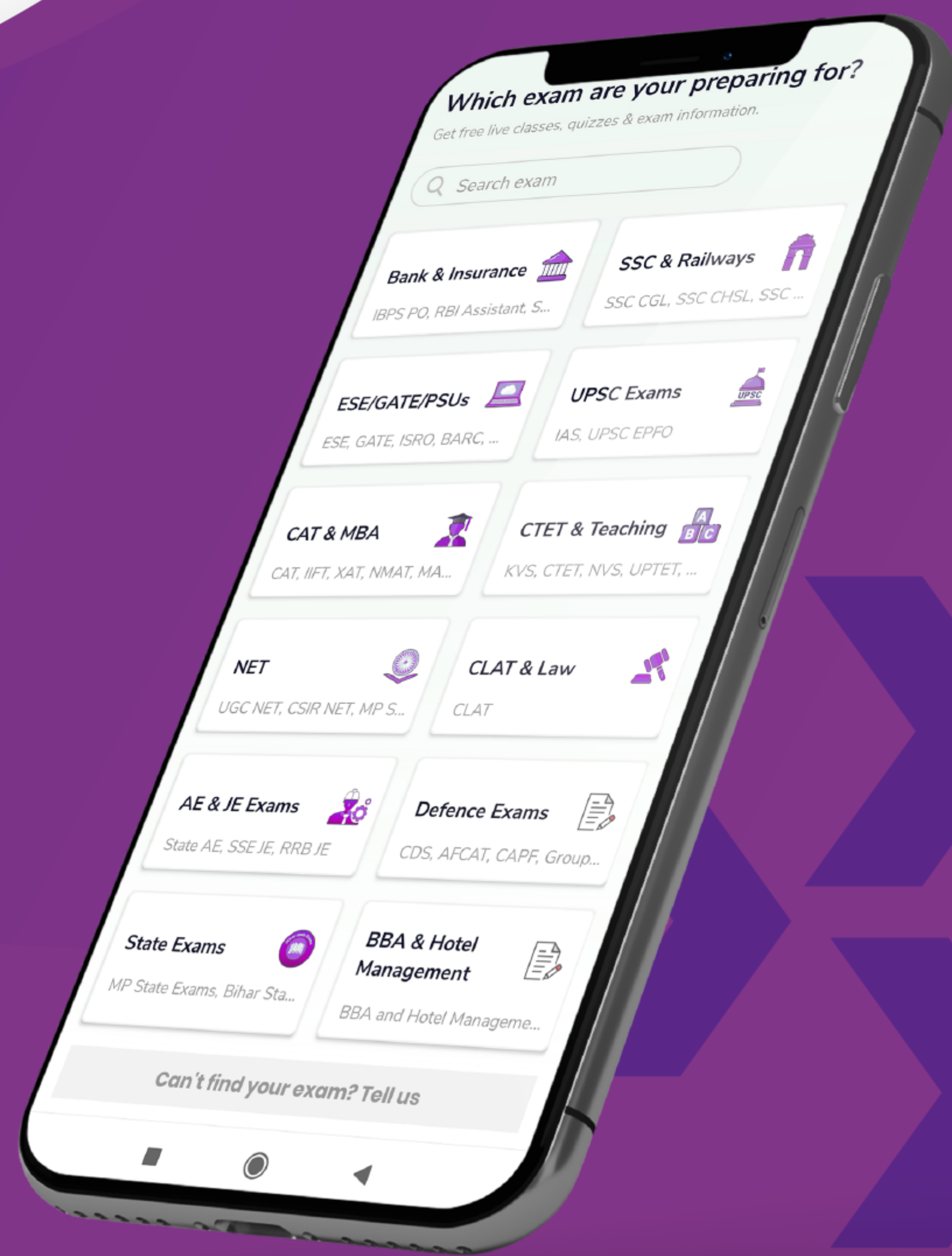


Angle between two lines: If two lines having slopes  $m_1$  and  $m_2$  then angle between the two lines is given by



$$\tan\theta = \pm \frac{m_2 - m_1}{1 + m_1 m_2} \text{ where } m_1, m_2 = \text{slope of the lines}$$

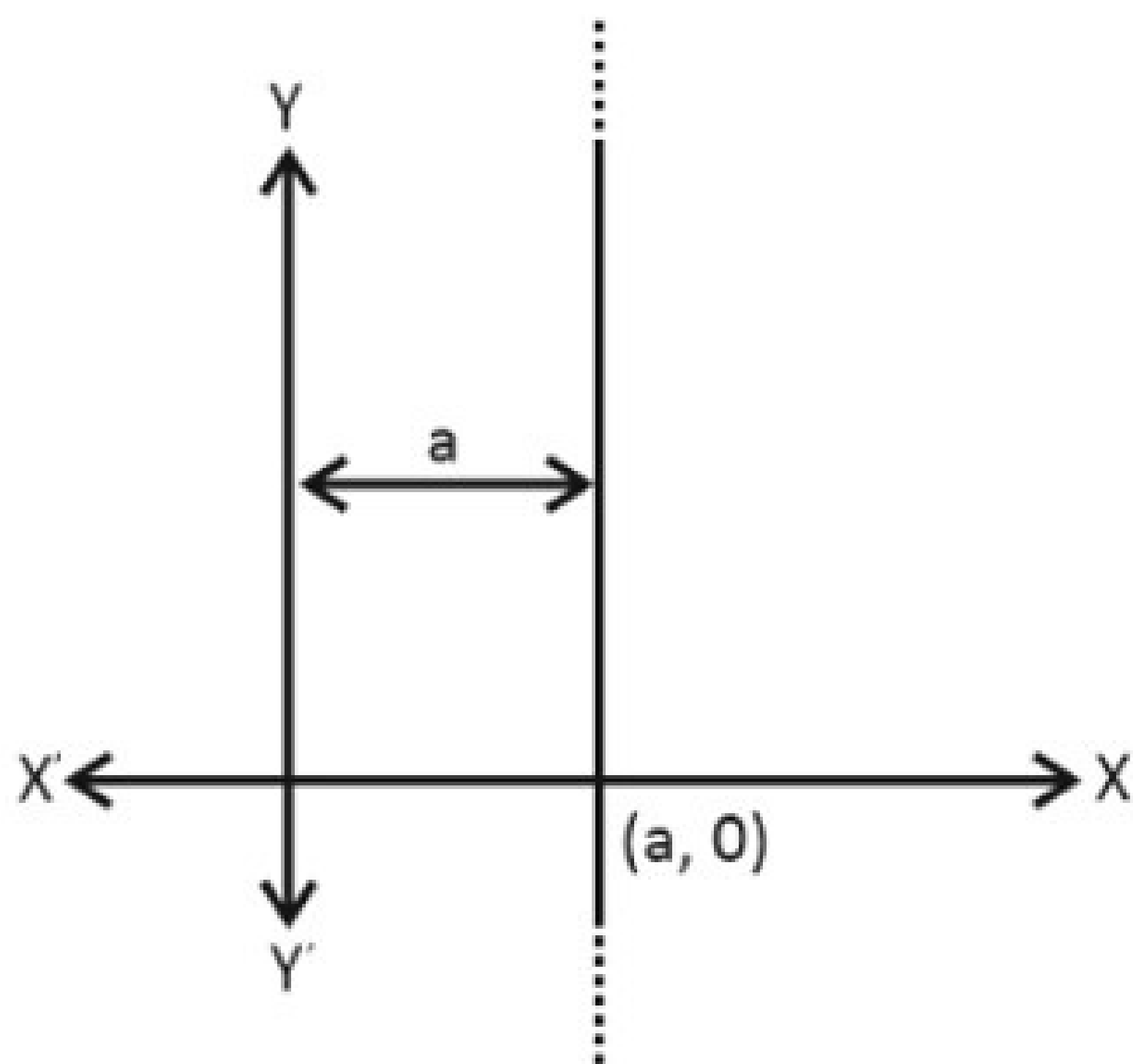
$$\Rightarrow \theta = \tan^{-1} \left( \frac{m_2 - m_1}{1 + m_1 m_2} \right)$$



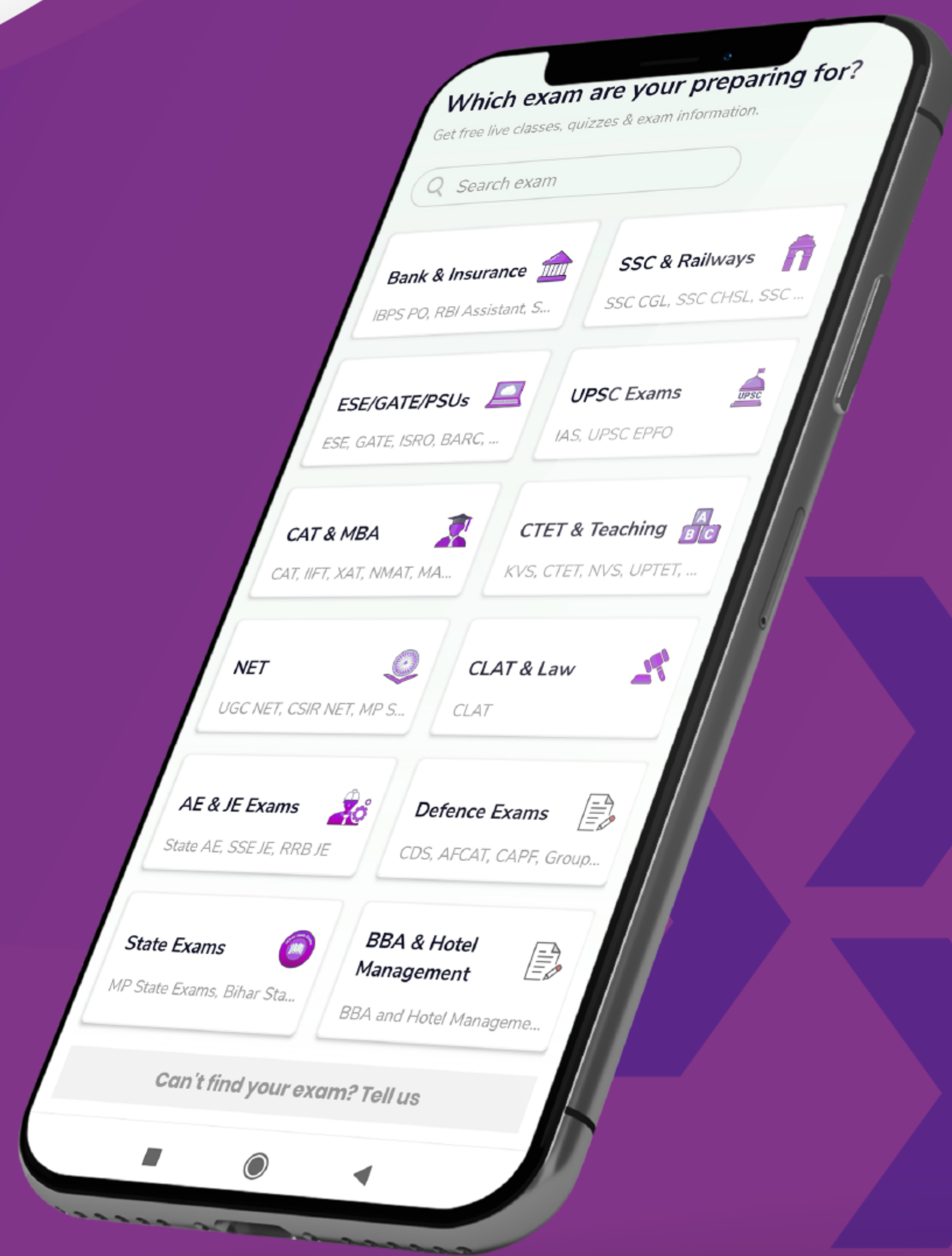
Note: If lines are parallel to each other then  $\tan\theta = 0^\circ$

If lines are perpendicular to each other then  $\cot\theta = 0^\circ$

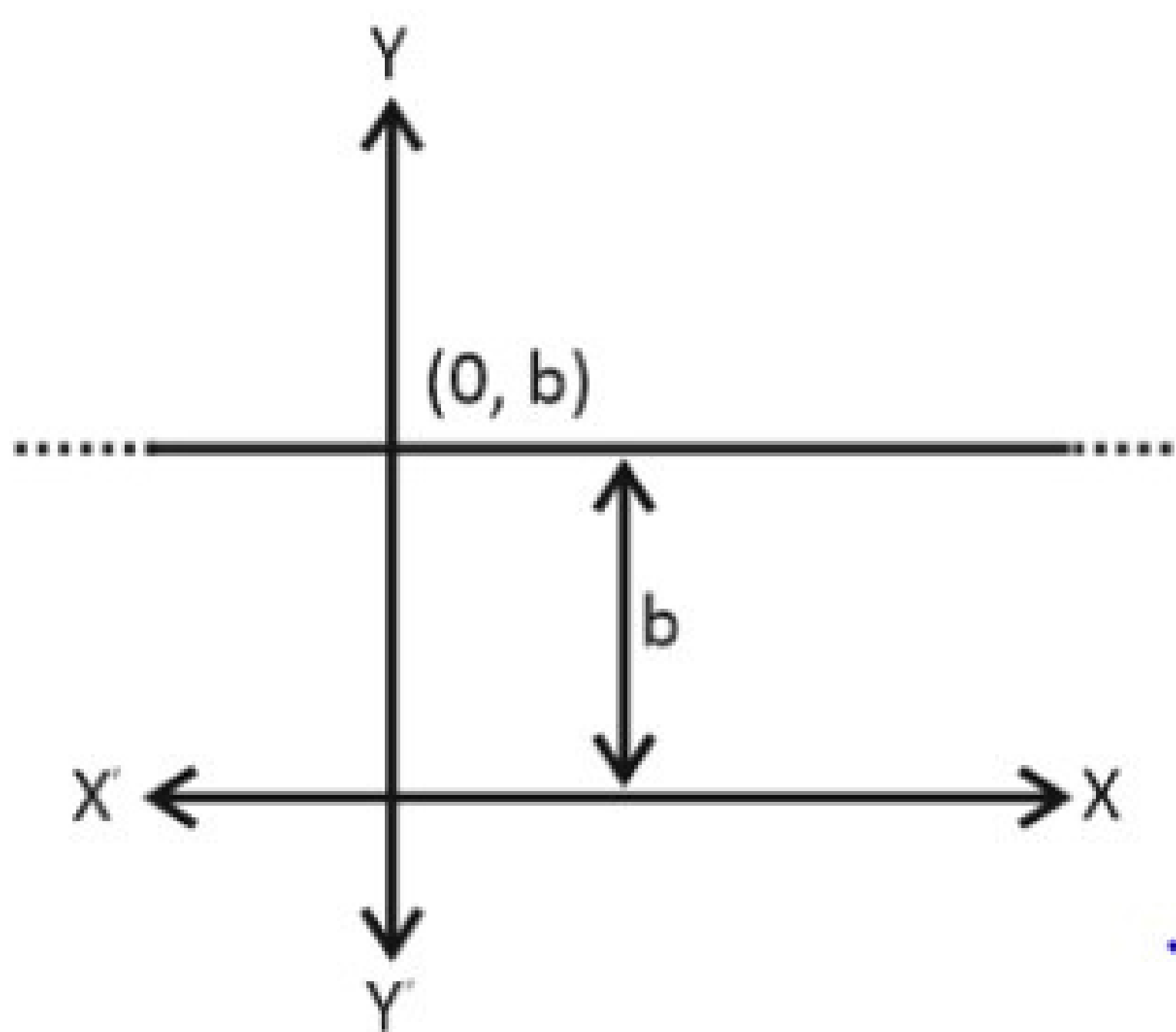
Equation of line parallel to y-axis: The equation of a straight line to the x -axis and at a distance a from it, is given by  $X = a$ .

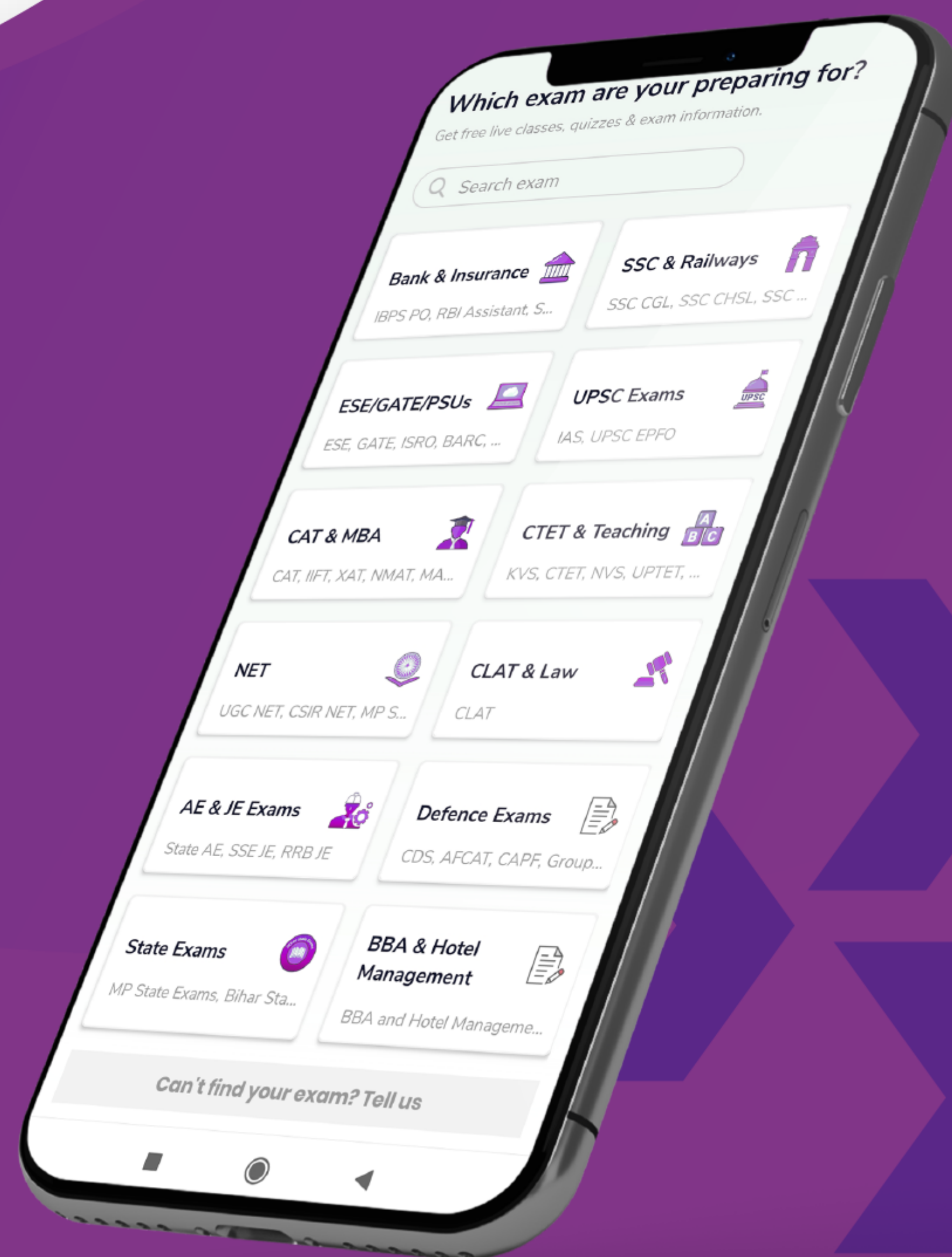






Equation of line parallel to x-axis: The equation of a straight line parallel to the y- axis and at a distance a from is given by  $Y = b$ .

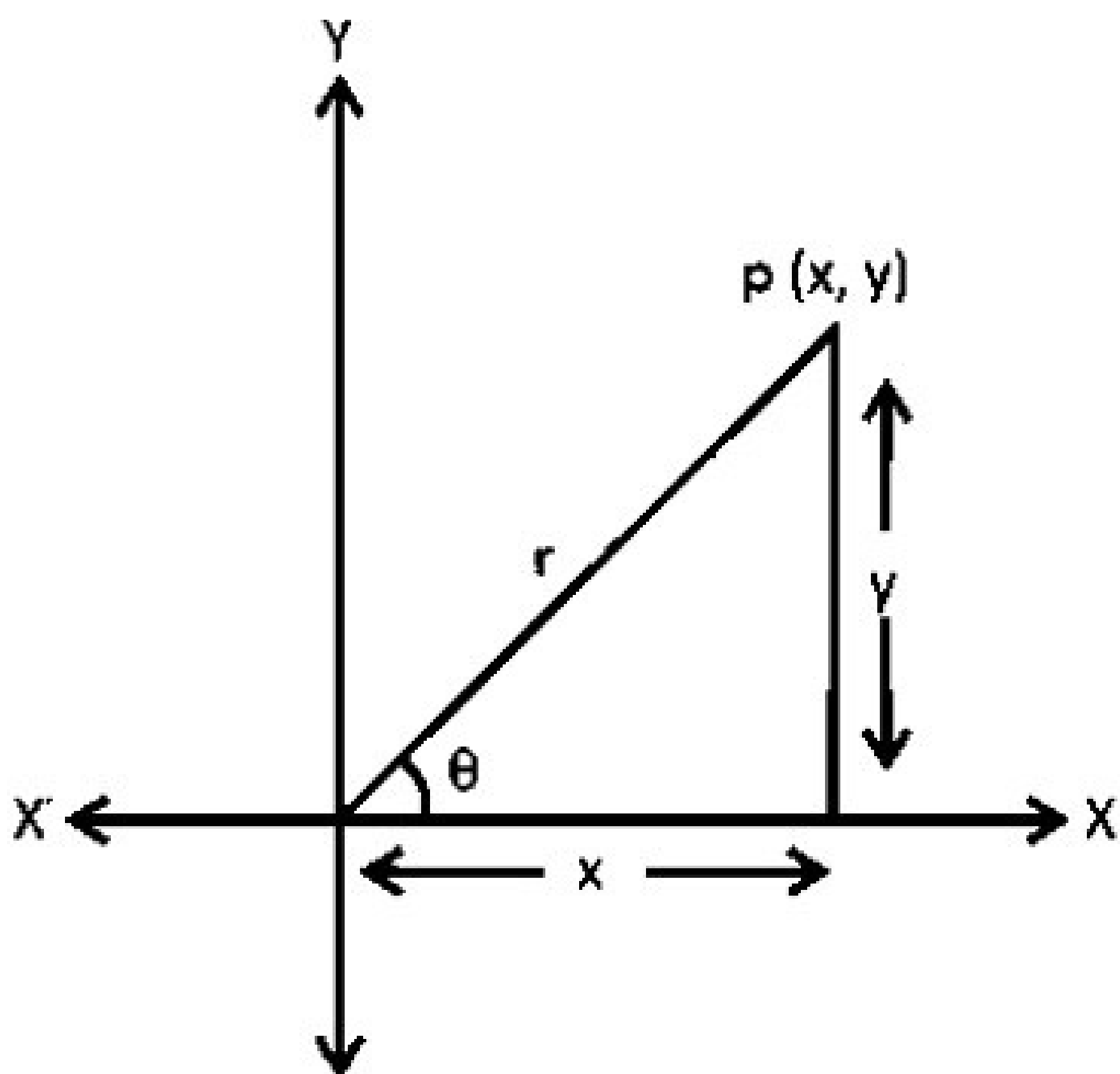




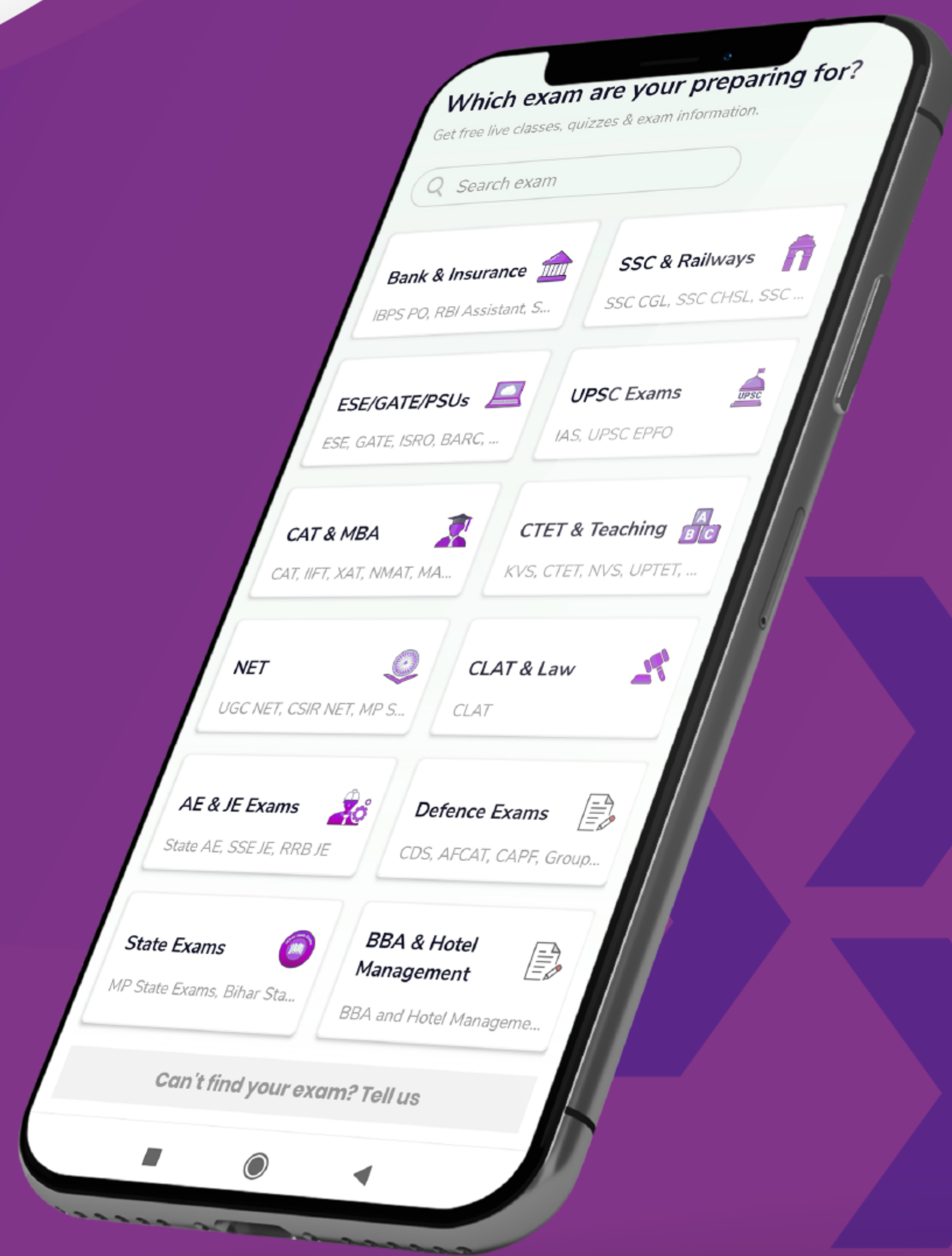
## Different types of Equations of line:

1. Normal equation of the line:  $ax + by + c = 0$  Note: Area of the triangle formed by co-ordinate axes and the line  $ax + by + c = 0$  is given by  $\frac{c^2}{2ab}$ .

2. Polar Form of an equation:



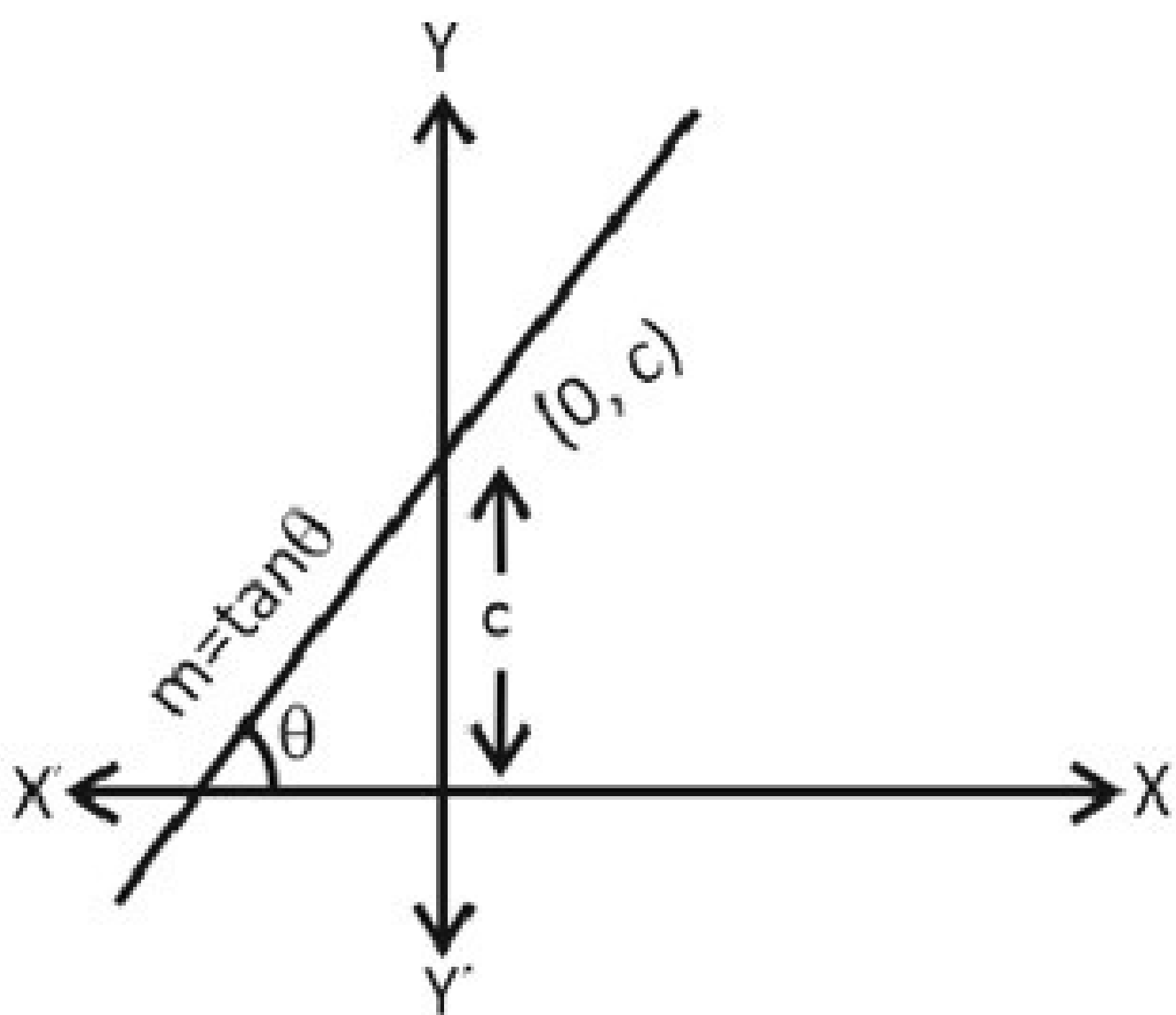


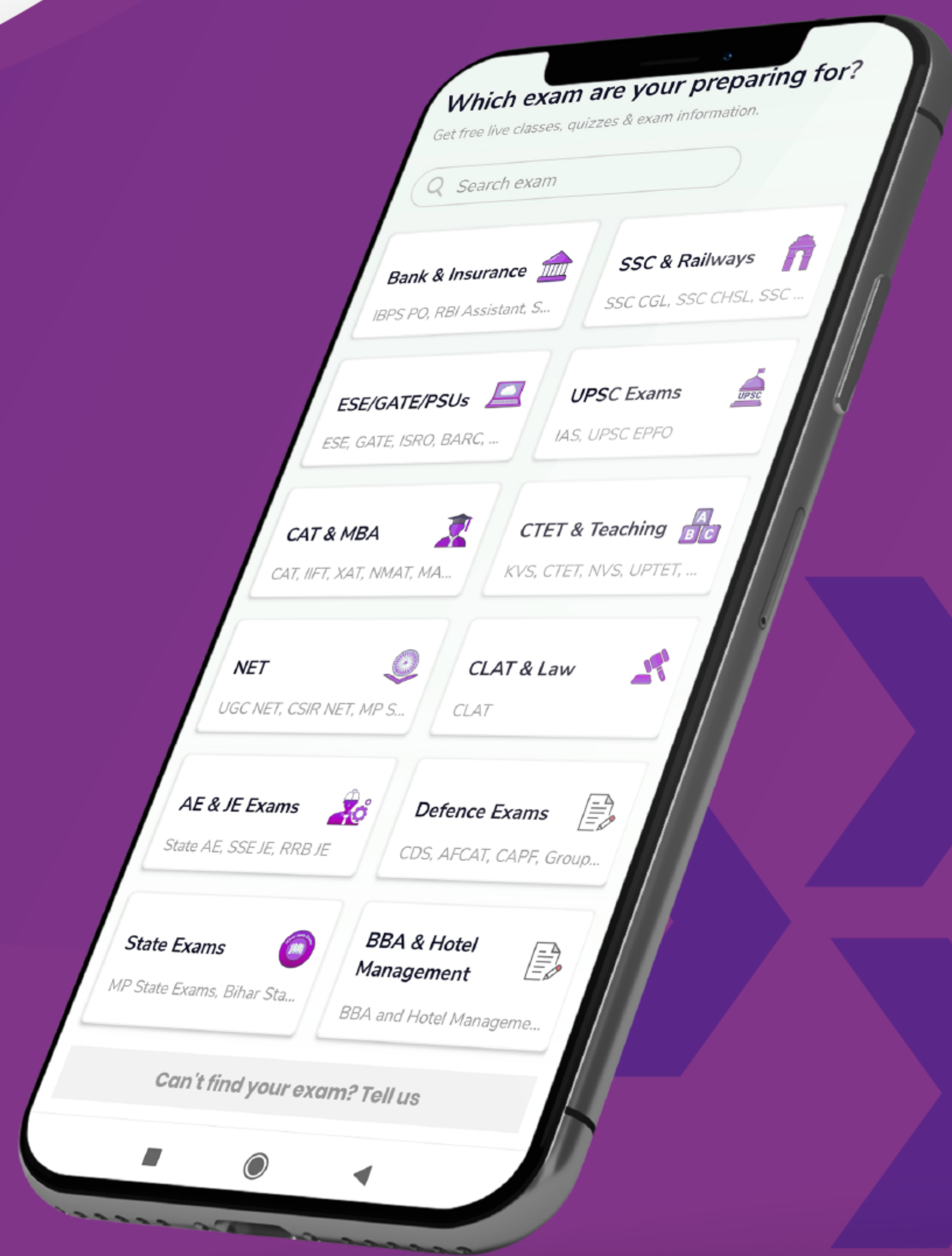


$$r = \sqrt{x^2 + y^2} ; \sin \theta = \frac{y}{r} \Rightarrow y = r \cdot \sin \theta ; \cos \theta = \frac{x}{r} \Rightarrow x = r \cdot \cos \theta$$

Co-ordinates of points in Polar Form: **(rSin  $\theta$ , rCos  $\theta$ )**

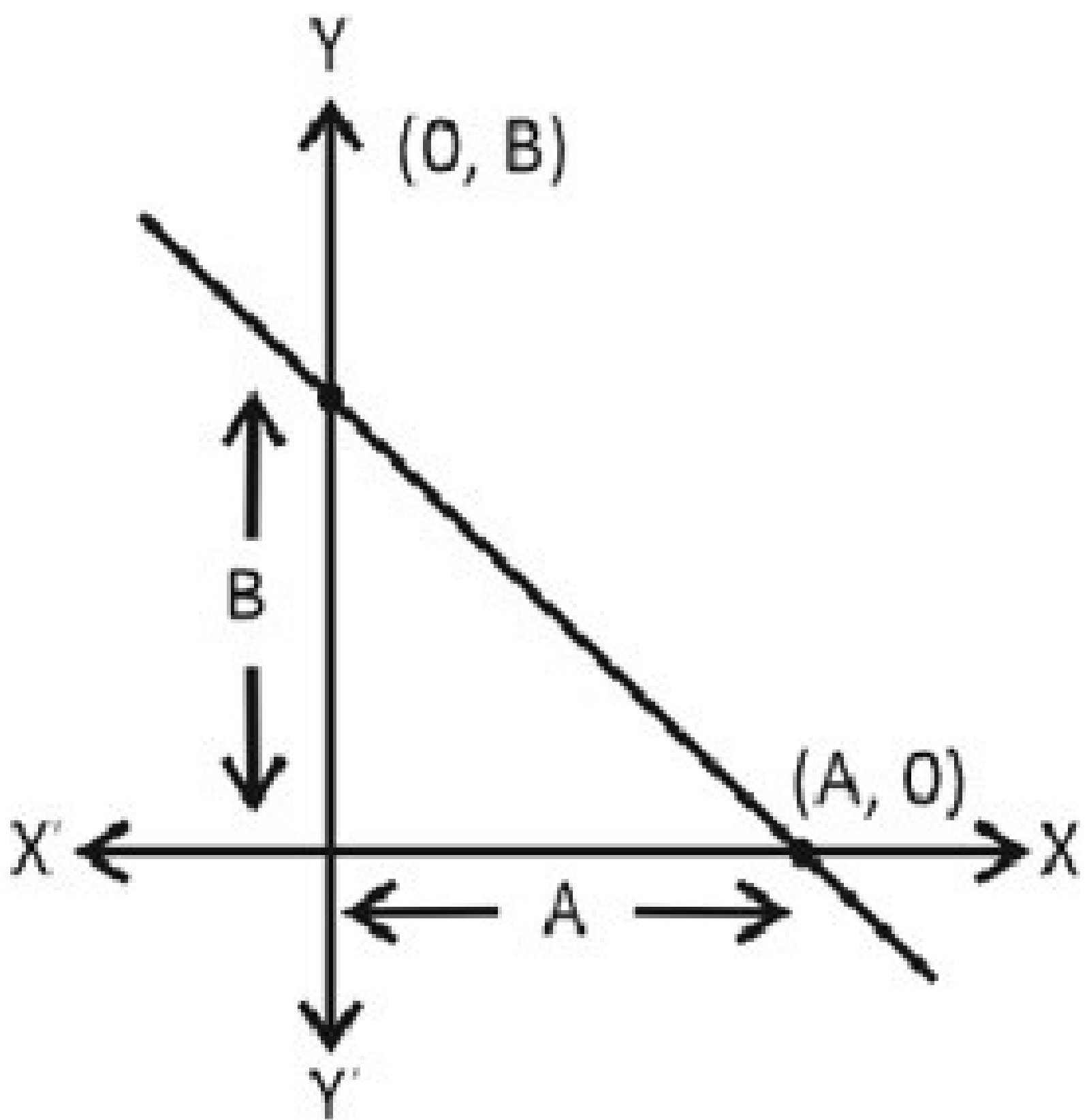
**3. Slope – Intercept Form:**  $y = mx + c$  Where,  $m$  = slope of the line &  $c$  = intercept on Y-axis



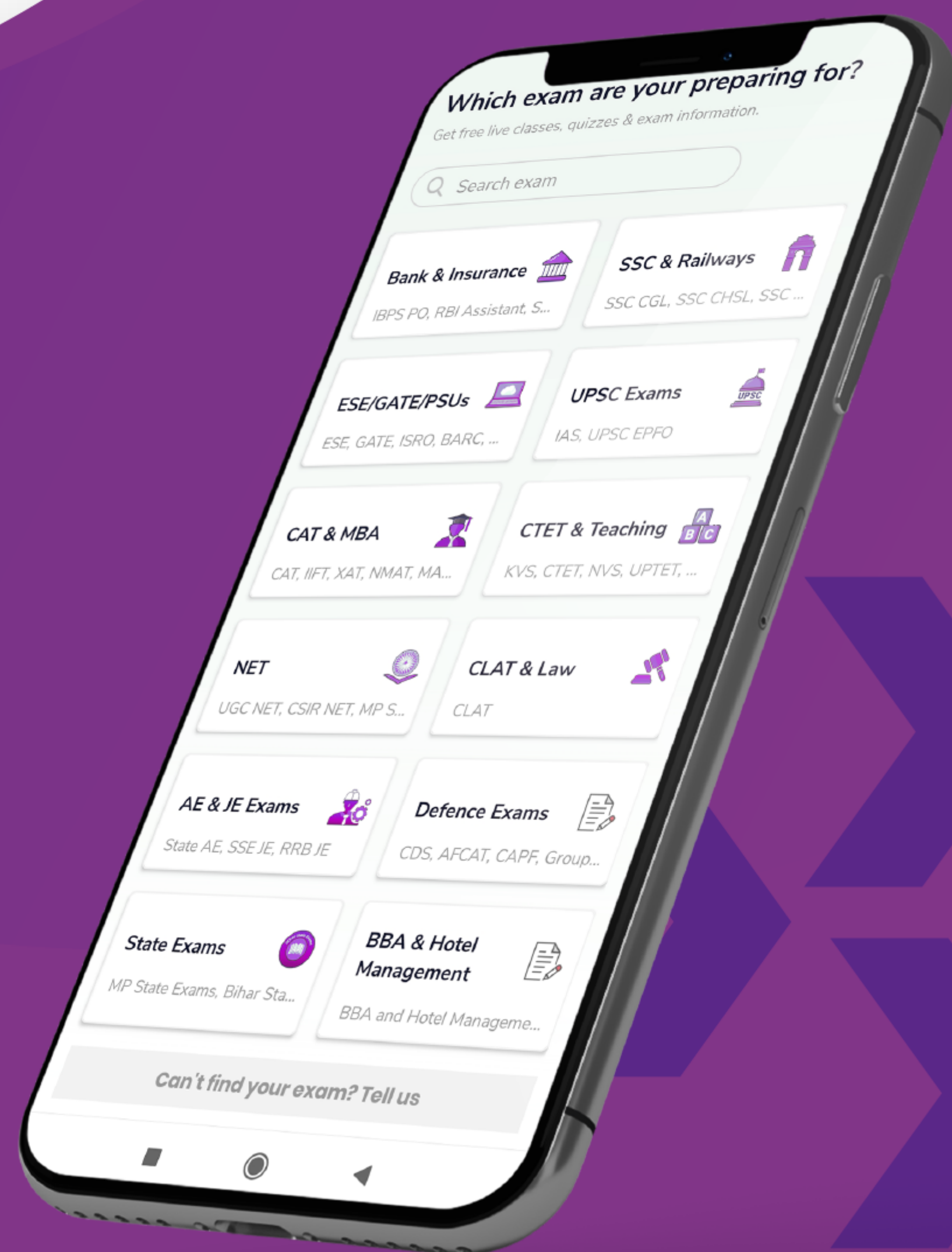


#### 4. Intercept Form:

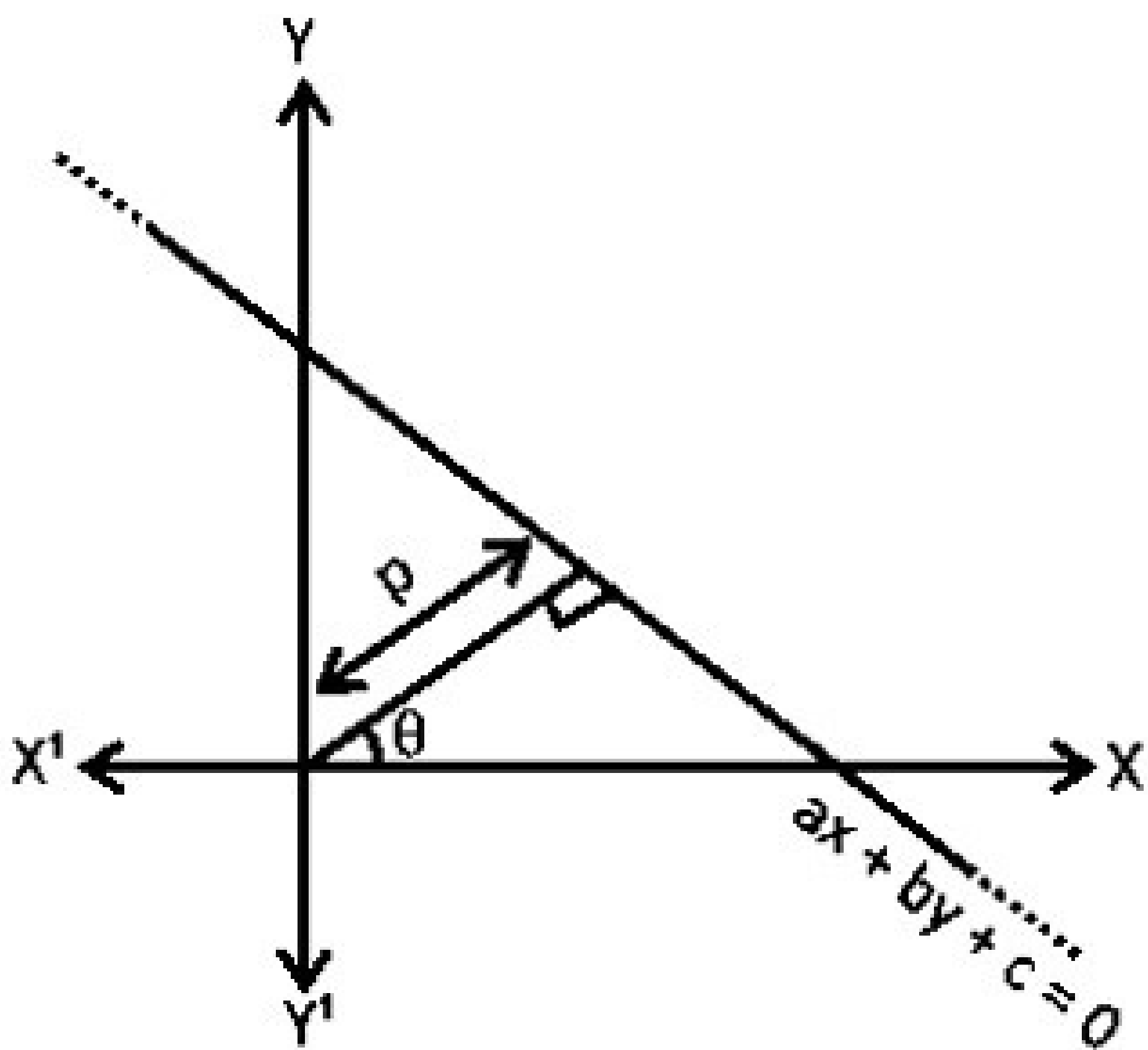
$\frac{x}{A} + \frac{y}{B} = 1$ , Where, A and B are x – intercept and y – intercept respectively .





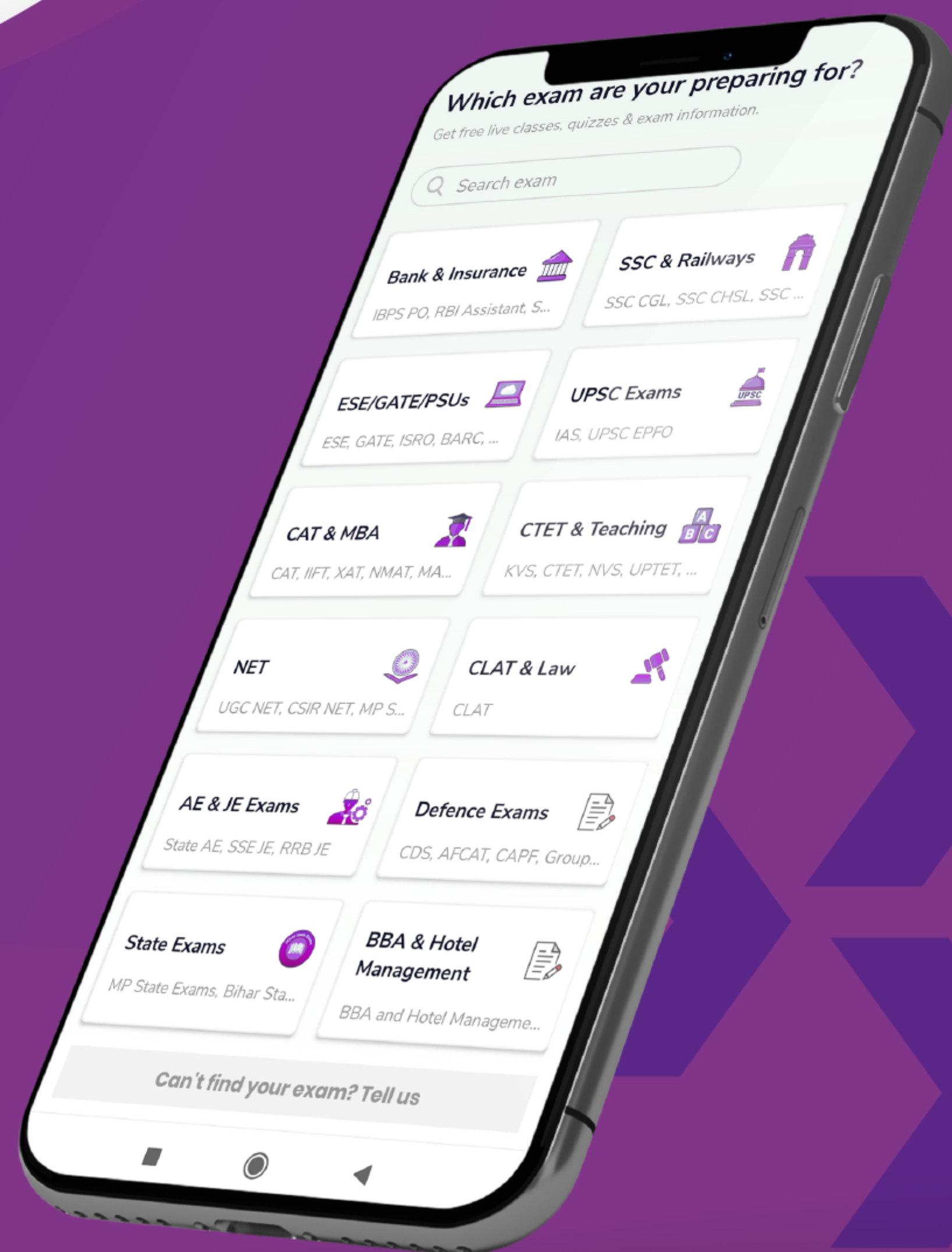


## 5. Trigonometric form of equation of line, $ax + by + c = 0$

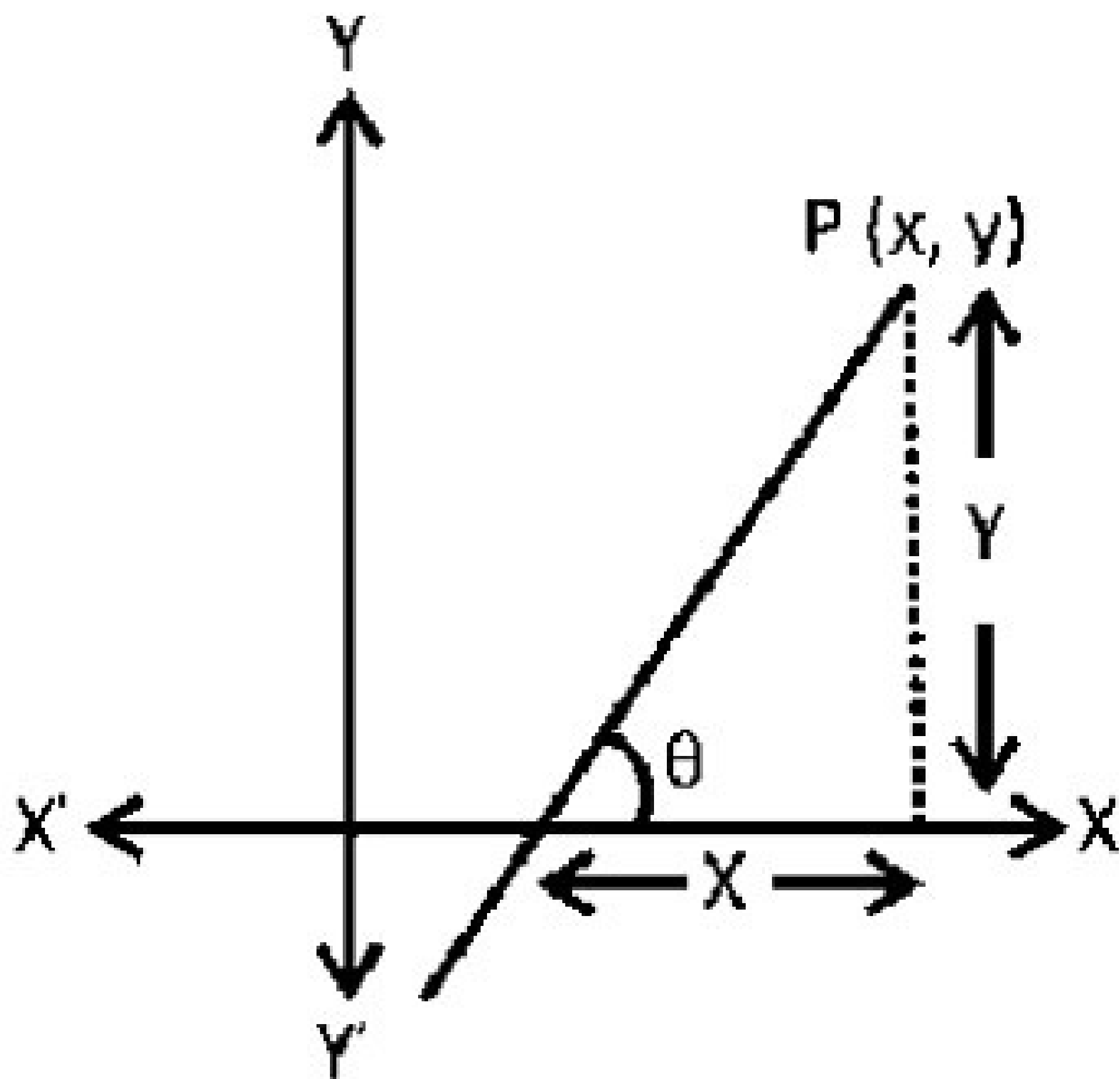


$$x \cos \theta + y \sin \theta = p,$$

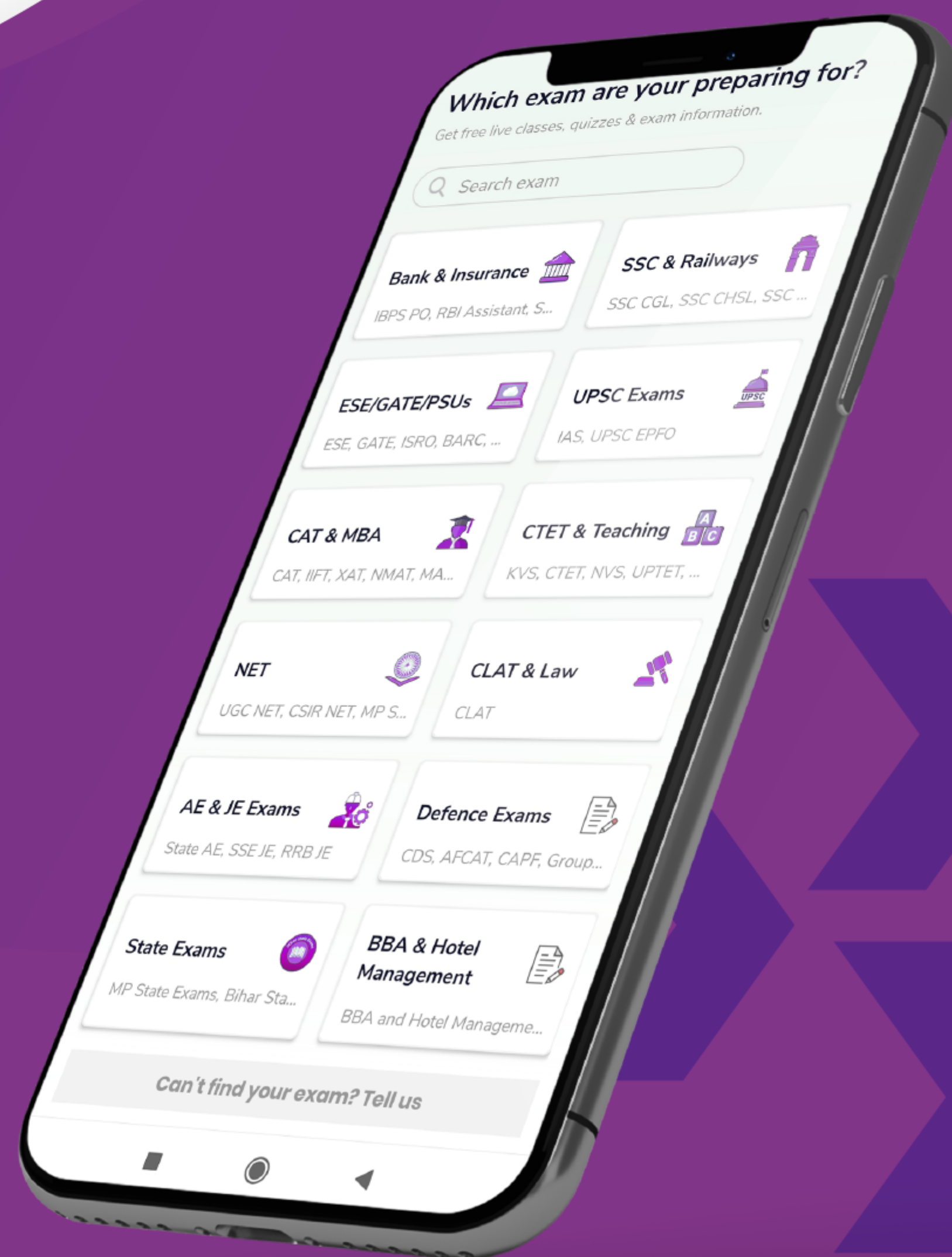
$$\text{Where, } \cos \theta = -\frac{a}{\sqrt{a^2 + b^2}}, \sin \theta = -\frac{b}{\sqrt{a^2 + b^2}} \text{ and } p = \frac{c}{\sqrt{a^2 + b^2}}$$



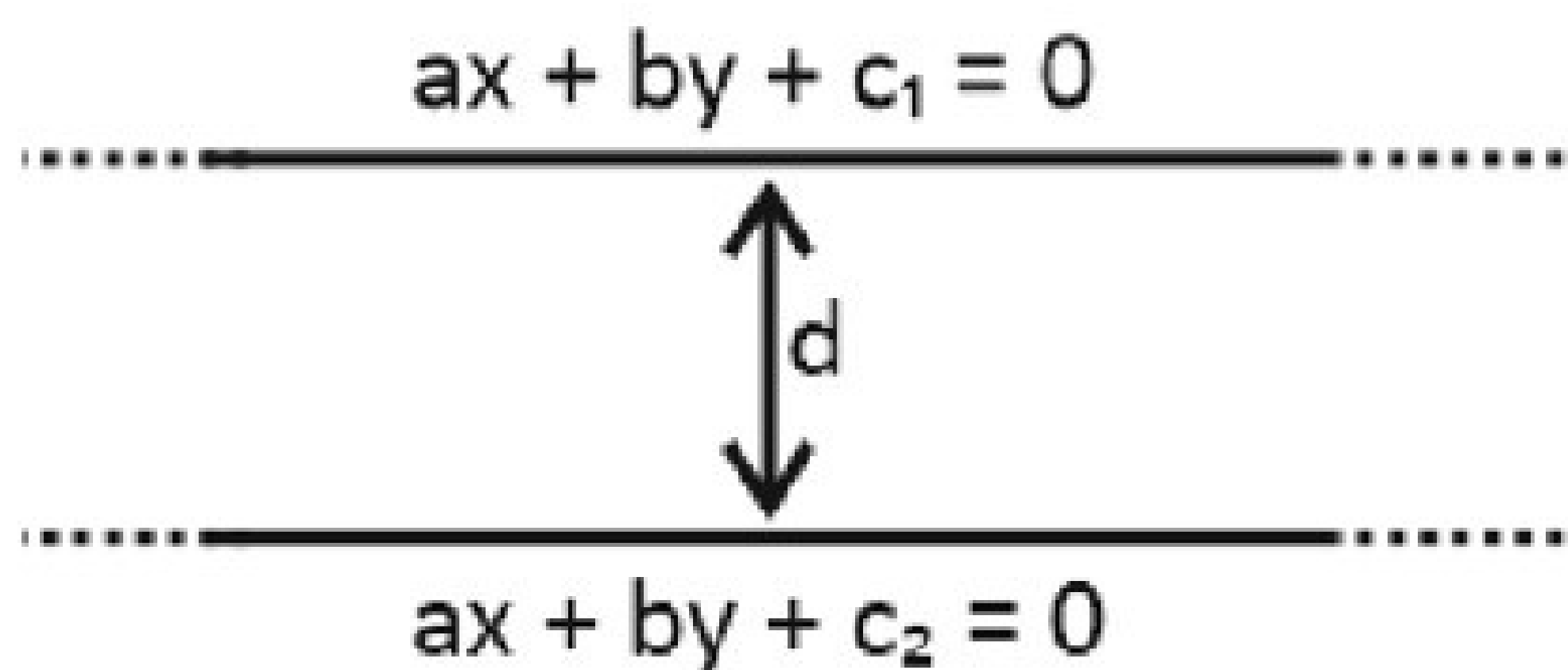
6. Equation of line passing through point  $(x_1, y_1)$  & has a slope “m”:  $y - y_1 = m(x - x_1)$







**7. Equation of two lines parallel to each other:** Here,  $ax + by + c_1 = 0$  and  $ax + by + c_2 = 0$  represent the equations of two lines parallel to each other. “d” represent the distance between the two parallel lines.

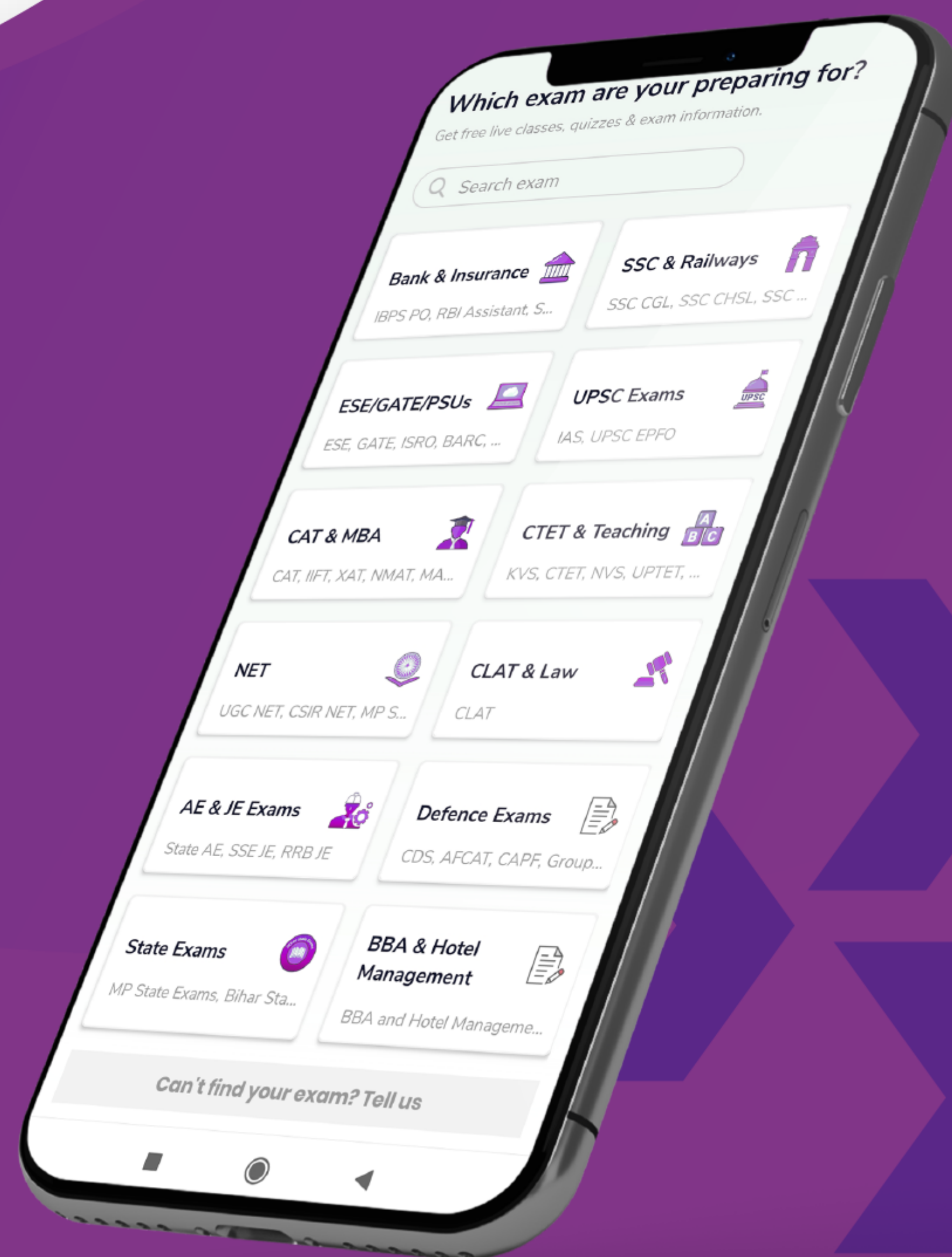


Note: Here, coefficient of x & y will be same

**8. Equation of two lines perpendicular to each other:**

$$ax + by + c_1 = 0$$

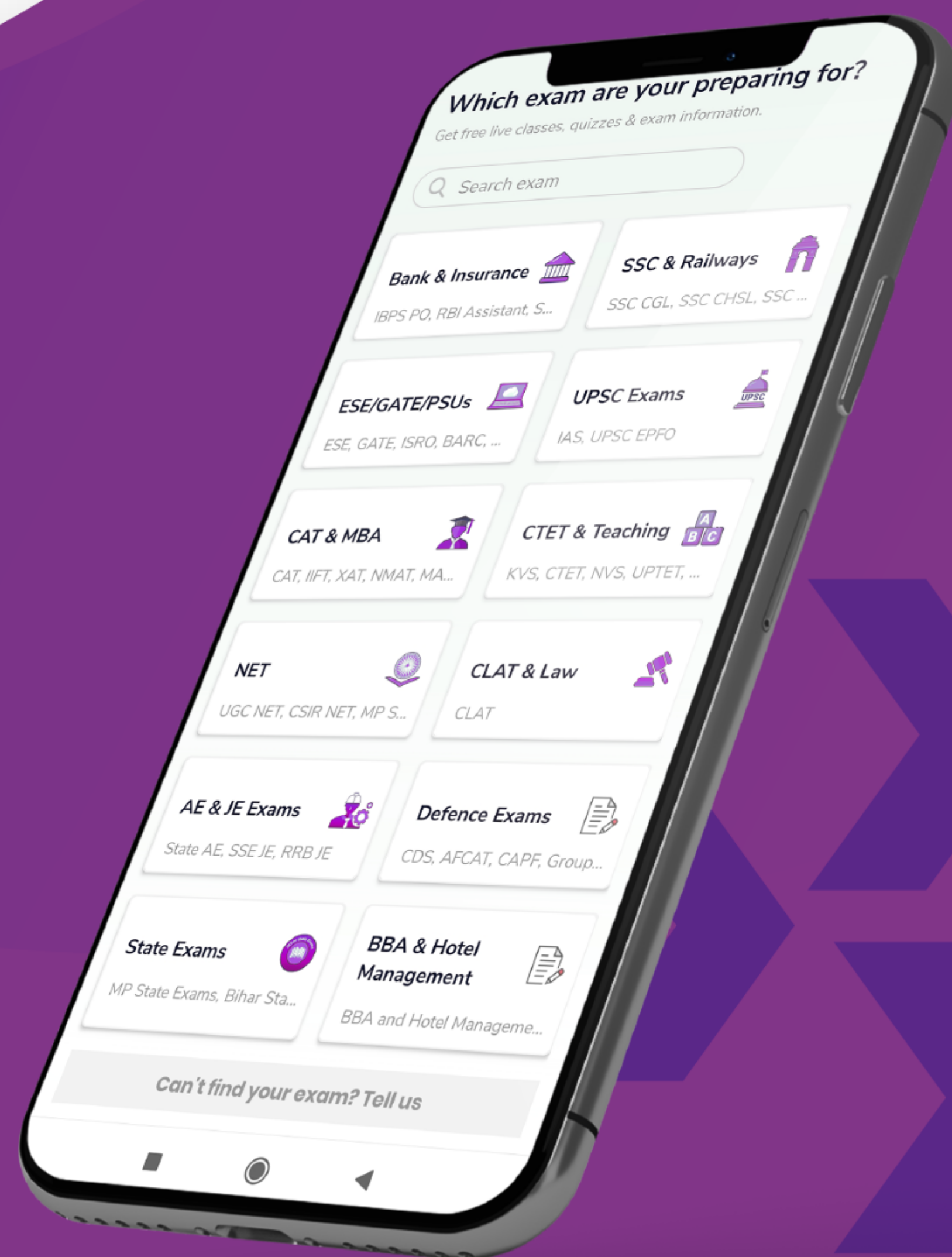
$$bx - ay + c_2 = 0$$



Note: Here, coefficient of  $x$  &  $y$  are opposite & in one equation there is negative sign. Note: If  $m_1, m_2$  are slopes of two perpendicular lines then  $m_1.m_2 = -1$ . The Distance of a Point from a Line: The length of perpendicular from a point  $A(x_1, y_1)$  to a line with equation  $ax + by + c = 0$  is:

$$p = \frac{|ax_1 + by_1 + c|}{\sqrt{a^2 + b^2}}$$





The Distance between two parallel lines: When two parallel straight lines with equations  $ax + by + c_1 = 0$  and  $ax + by + c_2 = 0$ , then the distance between them is given by:

$$\begin{array}{c}
 \text{.....} \overline{ax + by + c_1 = 0} \text{.....} \\
 \updownarrow d \\
 \text{.....} \overline{ax + by + c_2 = 0} \text{.....} \\
 d = \frac{|c_1 - c_2|}{\sqrt{a^2 + b^2}}
 \end{array}$$

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