

GATE 2021

Instrumentation Engineering

Questions & Answers (Memory Based)



1. A infinitely long line, with uniform positive charge density, lies along the z-axis. In cylindrical coordinates (r, ϕ, z) , at any point \vec{p} not on the z-axis, the direction of the electric field is

A. \hat{r}

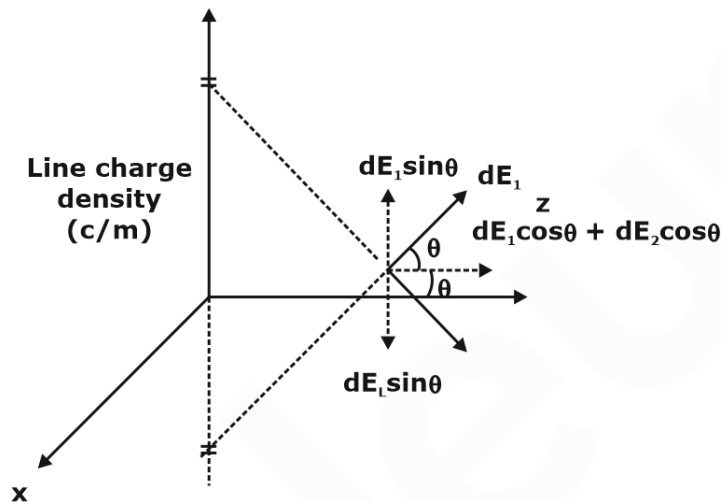
B. $\frac{\hat{r} + \hat{z}}{\sqrt{2}}$

C. $\hat{\phi}$

D. \hat{z}

Ans. A.

Sol.



2. Consider a system with transfer function $G(s) = \frac{2}{s+1}$, A unit step function $\mu(t)$ is applied to the system, which results in an output $y(t)$. If $e(t) = y(t) - \mu(t)$, then $\lim_{t \rightarrow \infty} e(t)$ is _____

Sol. $G(s) = \frac{2}{s+1}$ unit step is applied to this system.

Output

$$y(s) = \frac{2}{s(s+1)} = \frac{K_1}{s} + \frac{K_2}{s+1} = \frac{2}{s} - \frac{2}{s+1}$$

Inverse laplace transform

$$y(t) = 2u(t) - 2e^{-t}u(t)$$

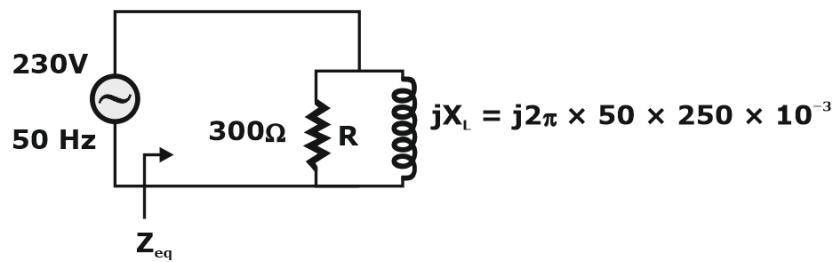
$$e(t) = y(t) - u(t) = (2 - 2e^{-t})u(t) - u(t)$$

$$e(t) = (1 - 2e^{-t})u(t)$$

$$\lim_{t \rightarrow \infty} e(t) = -1$$

3. Single phase transformer has a magnetizing inductance of 250 mH and a core loss resistance of 300 Ω , referred to the primary side. When excited with a 230 V 50 Hz Sinusoidal supply the primary the power factor of the input current drawn, with secondary an open circuited _____ (round off to two decimal places)

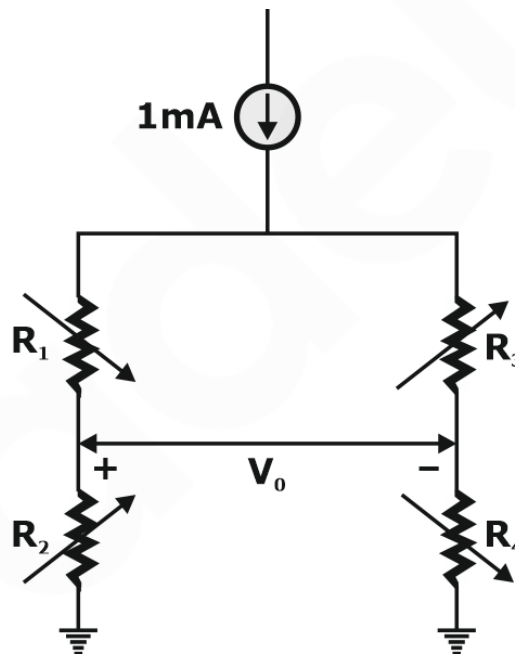
Sol. $Z_{eq} = \frac{R \times jX}{R + jX}$



$75.97 \angle 75.32^\circ$

$\cos(75.32^\circ) = 0.253$ lagg

4. For the full bridge made of linear strain gauges with gauge factor 2 as shown in the diagram, $R_1 = R_2 = R_3 = R_4 = 100 \Omega$ at 0°C . All strain gauges are made of same material and exposed to the same temperature. While measuring a strain of 0.01 of a temperature of 50°C , the output V_0 in millivolt is ____ (rounded off to two decimal places)



Sol. -2.5

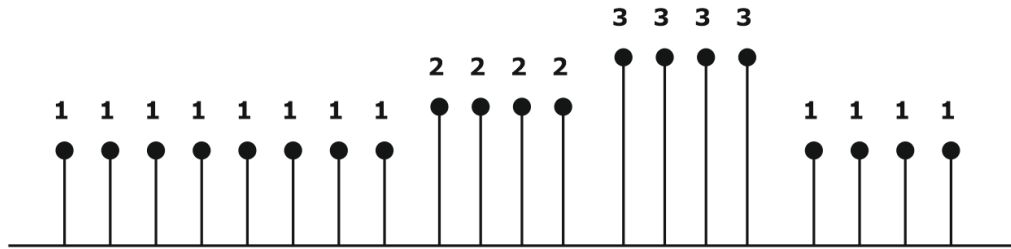
5. A 10 bit ADC has a full scale of 10 point 230 volt, when digital output is $(111111111)_2$. Quantization error of ADC mini volt is ____.

Sol. $\Delta = \text{Resolution} = \frac{V_{FS}}{2^n - 1} = \frac{10.230}{2^{10} - 1} = \frac{10.230}{1023} = 0.01$

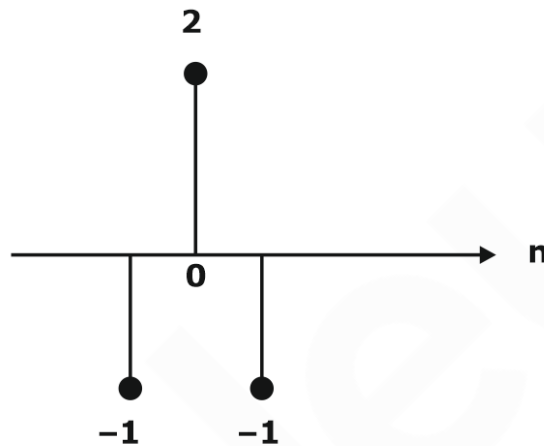
Quantization error $= \frac{\Delta}{2} = \frac{0.01}{2} = 0.005 = 5 \text{ m}$

Answer = 5

6. The input signal is shown below



Is passed through the filter with the following.



Sol. By tabulation method

	1	1	1	1	1	1	1	1	1	2	2	2	2	3	3	3	3	1	1	1	1
-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-2	-2	-2	-2	-3	-3	-3	-3	-1	-1	-1	-1
2	2	2	2	2	2	2	2	2	2	4	4	4	4	6	6	6	6	2	2	2	2
-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-2	-2	-2	-2	-3	-3	-3	-3	-1	-1	-1	-1

$$y[n] = \{-1, 1, 0, 0, 0, 0, 0, 0, 0, 0, -1, 1, 0, -1, 1, 0, 0, 2, 2, 0, 0, 3, -1\}$$

7. $y(t) = e^{-3t}u(t) * u(t + 3)$

Where * denotes convolution and $u(t)$ denotes the step function

The value of $y(t)$ as $t \rightarrow \infty$ is ____.

Sol. $y(t) = e^{-3t}u(t) u(t + 3)$

$$Y(s) = \frac{1}{s+3} \cdot \frac{e^{3s}}{s}$$

$$\lim_{t \rightarrow \infty} y(t) = \lim_{s \rightarrow 0} s \cdot Y(s) = \lim_{s \rightarrow 0} \frac{s \cdot e^{3s}}{s(s+3)} = \frac{1}{3} = 0.33$$

8. Let $u(t)$ denotes the unit step function the bilateral Laplace transformer of function $f(t) = e^t u(-t)$ is
- A. $1/s - 1$ with real part of $s > 1$ B. $1/s - 1$ with real part of $s < 1$
C. $-1/s - 1$ with real part of $s > 1$ D. $-1/s - 1$ with real part of $s < 1$ Ans. ?

Ans. D

Sol. $f(t) = e^t u(-t)$

Laplace transform

$$F(s) = \frac{-1}{s-1}, \quad \text{Re}\{s\} < 1$$

9. $\sqrt{2} \sin t$ ult, is applied to system with T.F. $a(s) = \frac{1}{s+1}$. Amplitude of S.S. o/p is _____.

Sol. $\sqrt{2} \sin \rightarrow \boxed{\frac{1}{s+1}} \rightarrow$

$$Y(w) = \sqrt{2} \sin t \cdot \frac{1}{j\omega + 1}$$

$$w = 1$$

$$y(w) = \sqrt{2} \sin t \cdot \frac{1}{j1 + 1}$$

$$y(t) = \frac{\sqrt{2}}{\sqrt{2}} \sin(t - 45^\circ)$$

$$y(t) = 1 \sin(t - 45^\circ)$$

$$\text{Amplitude} = 1$$

10. Tanking N as positive for cw encirclement the no. of encirclement of $[-1, 0]$ in the Nyquil.
Plot of $G(s) = \frac{3}{s-1}$ is _____.

Ans. -1

Sol.: $G(s) = \frac{3}{s-1} \rightarrow P_+ = 1 \rightarrow \text{No. of RHP Poles of } G(s)$

$$\text{CE: } 1 + GW = 0$$

$$1 + \frac{3}{s-1} = 0$$

$$s + 2 = 0$$

$$s = -2 \rightarrow \text{LHP}$$

so, RHP roots of CE = 0

$$\text{and } Z_+ = 0$$

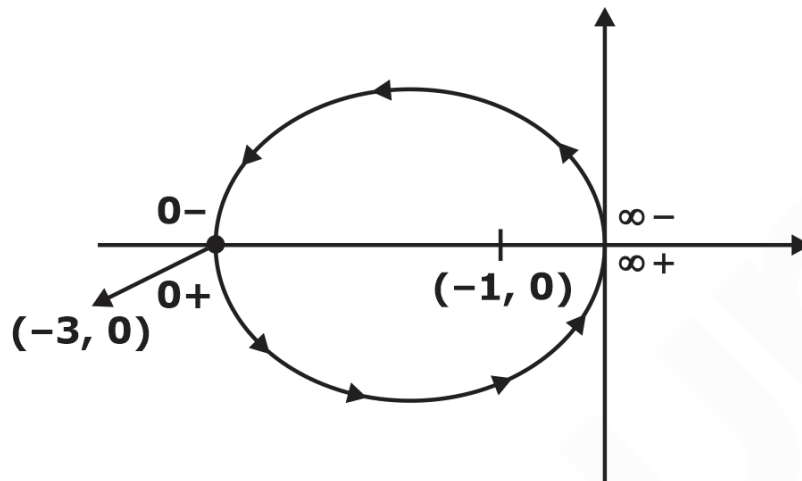
$$N = P_+ - Z_+$$

$$N = 1 - 0 = 1$$

But this "N" is with the ACW positive convention. Here, we need to take CW as positive.

So, $N = -1$

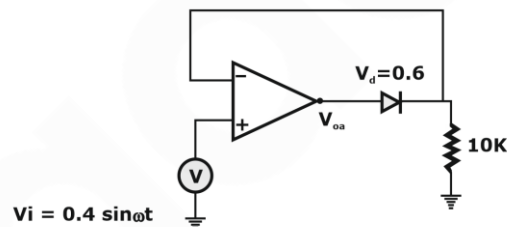
Alternate: Nyquist plot of $G(s)$ will be



Clearly one ACW encirclement

So, $N = -1$

11.



When V_i is at its peak, the value of $V_{oa} =$

Sol. For peak value of i/p i.e. $V_{imax} = 0.4 \text{ V}$

$$V_P = V_n = V_{imax} = 0.4 \text{ V}$$

∴ virtual short concept

Diode is FB

$$\therefore V_{oa} = V_D + V_0 = 0.6 + 0.4 = 1.0 \text{ V.}$$

12. A single phase T/F has has a max^m efficiency of 98% Core loss = 80 W, eq winding resistance as seen from the primary side 0.5Ω . I current 25A % of crated current at which η_{max} occurs.

$$x = \sqrt{\frac{\text{iron loss}}{\text{Fl copper}}} \times W_i = w_{cm}$$

Ans. 50.6

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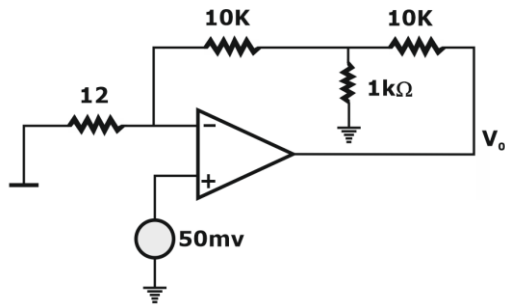
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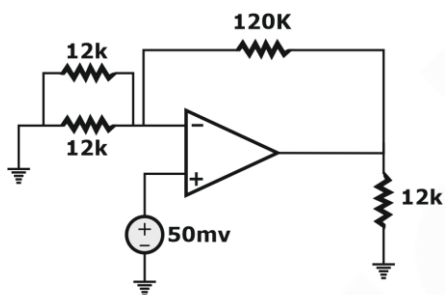
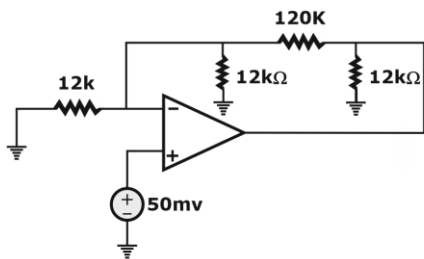
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13.



Sol. Using star to Delta.



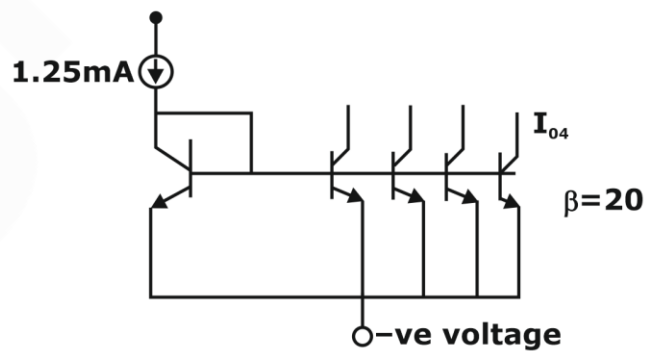
$$V_o = [1 + R_f/R_1]V_i = [1 + 120/(12/12)] \times 50$$

$$= 1050 \text{ mV}$$

$$= 1.05 \text{ V}$$

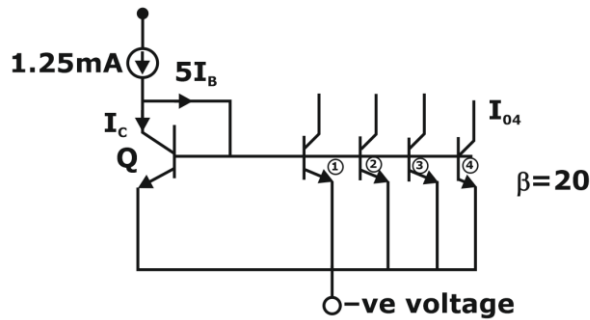
$$V_o \cong 1 \text{ volt}$$

14.



Find value of $i_{o4} = \text{mA}$

Sol.



Q 1 2 3 4 are identical transistors.

$$\therefore \beta_1 = \beta_2 = \beta_3 = \beta_4 = \beta_Q = 20$$

$$I_{B1} = I_{B2} = I_{B3} = I_{B4} = I_{BQ}$$

$$\therefore I_{O4} = I_{O3} = I_{O2} = I_{O1} = I_{BQ}$$

$$I_{ref.} = I_{CQ} + 5I_B$$

$$I_{ref.} = \beta I_B + 5I_B = 20 I_B + 5I_B = 25 I_B$$

$$1.25 = 25I_B$$

$$\Rightarrow I_B = \frac{1.25}{25}$$

$$I_{O4} = I_{C1} = \beta I_{B1} = 20 \times \frac{1.25}{25} = 1\text{mA}$$

15. A house hold fan concurs 60w an draws a current of 0.3125A when connected to 230 r.m.s. AC, 50Hz Q = ?

Sol. $P = V.I \cos\phi$

$$60 = 230 \times 0.3125 \times \cos\phi$$

$$\cos\phi = 0.83$$

$$Q = V.I.\sin(\cos^{-1}0.831)$$

$$Q = 39.57 \text{ VAR}$$

16. A slep ring Induction machine is started by an extrunal resistance so advantage of external resistance added is

A. Pf at starting is lower

B. Starting torque is high

C. Losses at starting is lower

D. Starting current is higher

Sol. $\downarrow I_{st} = \frac{V}{Z} \uparrow$

$$\uparrow I \cos\phi = \frac{R}{Z}$$

$$\uparrow I_{st} \propto (R_2 + R_{ex}) \uparrow$$

$$\downarrow \text{losses} \propto I_2^2 R_{02}$$

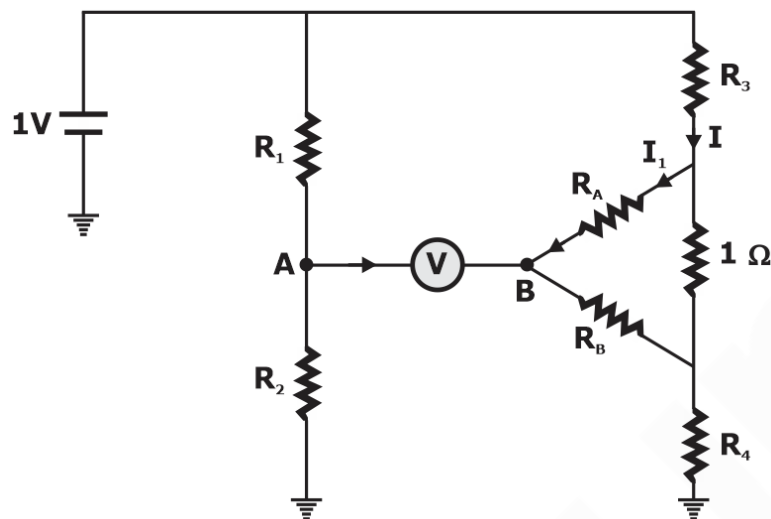
B and C are correc.



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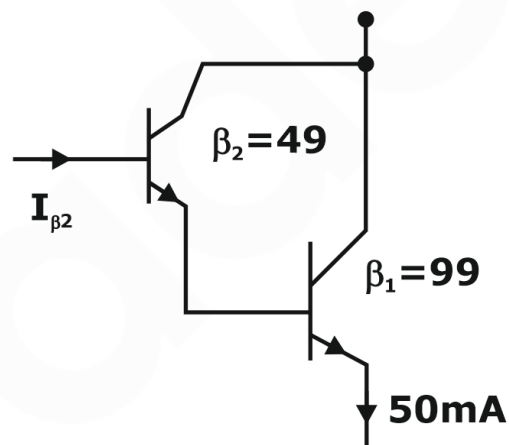
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18. In the bridge circuit shown, the voltmeter V showed zero when the value of the resistors are $R_1 = 100\Omega$, $R_2 = 100\Omega$, $R_3 = 90\Omega$, If $\left(R_1 / R_2 = \frac{R_A}{R_B}\right)$ the value of R_4 in ohms is _____.

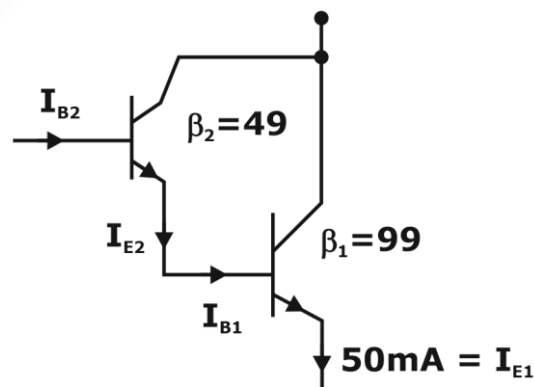


Ans. 99

19. The transistor Q_1 has gain $\beta_1 = 99$ and Q_2 has $\beta_2 = 49$, the current $I_{\beta 2}$ is _____ μA .



Sol. ?



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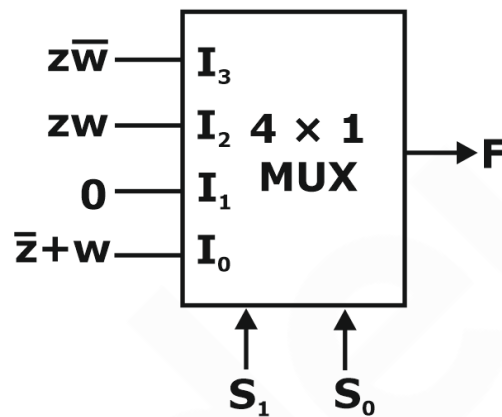
$$I_{E1} = (1 + \beta) I_{B1}$$

$$I_{B1} = I_{E2} = (1 + \beta_2) I_{B2}$$

$$\therefore I_{E1} = (1 + \beta_1) (1 + \beta_2) I_{B2}$$

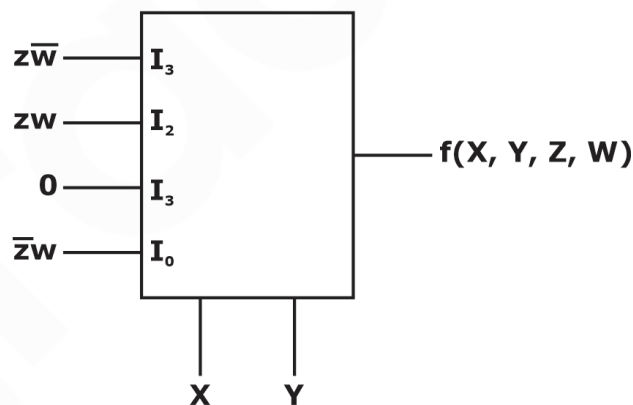
$$I_{B2} = \frac{50}{100 \times 50} = 0.01 \text{mA}$$

20. 4×1 multiplexer with two selection line is used to realize Boolean function F having four Boolean variable x, y, z, w as shown, S_0, S_1 denotes the LSB and MSB of selection lines of multiplexer. I_0, I_1, I_2, I_3 are input line, The canonical sum of product of F is
- A. $F(x, y, z, w) = \sum m(2, 5, 9, 11, 14)$ B. $F(x, y, z, w) = \sum m(0, 1, 3, 14, 15)$
 C. $F(x, y, z, w) = \sum m(0, 1, 3, 11, 14)$ D. ?



Ans. C

Sol.



$$f = \bar{x}\bar{y}(\bar{z} + w) + x\bar{y}zw + xyz\bar{w} = \bar{x}\bar{y}\bar{z} + \bar{x}\bar{y}w + x\bar{y}zw + xyz\bar{w}$$

$$f = \bar{x}\bar{y}\bar{z}(\bar{w} + w) + \bar{x}\bar{y}(\bar{z} + z)w + x\bar{y}zw + xyz\bar{w}$$

$$f = \bar{x}\bar{y}\bar{z}\bar{w} + \bar{x}\bar{y}\bar{z}w + \bar{x}\bar{y}z\bar{w} + \bar{x}\bar{y}zw + x\bar{y}z\bar{w} + xyz\bar{w}$$

$$f = \sum m(0, 1, 3, 11, 14)$$

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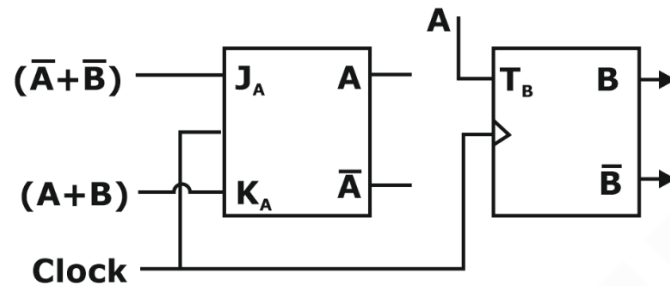
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21. Given block diagram of synchronous sequential circuit with one JK-flip flop and one T-flip flop with their output denoted as A and B respectively with $J_A = (\bar{A} + \bar{B})$, $K_A = (A + B)$ and $T_B = A$, starting and initial state $AB = 00$, the sequence of states AB visited by the circuit.

- A. $00 \rightarrow 10 \rightarrow 11 \rightarrow 01 \rightarrow 00$ B. $00 \rightarrow 01 \rightarrow 10 \rightarrow 11 \rightarrow 00$
C. $00 \rightarrow 10 \rightarrow 01 \rightarrow 11 \rightarrow 00$ D. ?



Ans. C

Sol.

Present State		J_A	K_A	$T_B = A$	Next State	
A	B	$\bar{A}\bar{B}$	$A + B$		A	B
0	0	1	0	0	1	0
1	0	1	1	1	0	1
0	1	1	1	0	1	1
1	1	0	1	1	0	0

$00 \rightarrow 10 \rightarrow 01 \rightarrow 11 \rightarrow 00$

22. For a 4-bit flash type Analog to Digital Converter (ADC) with full scale input voltage range 'V' which of the following statement is/are correct?
- A. The ADC requires one 4 to 2 priority encoder and 4 comparators
B. The ADC requires 15 comparators
C. A change in input voltage by $V/16$ will always flip MSB of the output
D. A change in the input voltage by $V/16$ will always flip the LSB of the output

Ans. B & D

Sol. For 'n' bit flash type ADC

Number of comparator $n^n - 1$

Number of Resistance = 2^n

Priority Encoder = $2^n \times n$

23. When the movable arm of a Michelson interferometer in vacuum ($n = 1$) is moved by $325 \mu\text{m}$, the number of fringe crossing is 1000. The wavelength of the laser used in nanometer is _____

Ans. 650

24. Let $f(z) = \frac{1}{z^2 + 6z + 9}$ defined in the complex plane. The integral $\oint_C f(z)dz$ over the contour of a circle C with centre at the origin and unit radius is_____.

Sol. Given

Poles of $f(z)$ are given by,

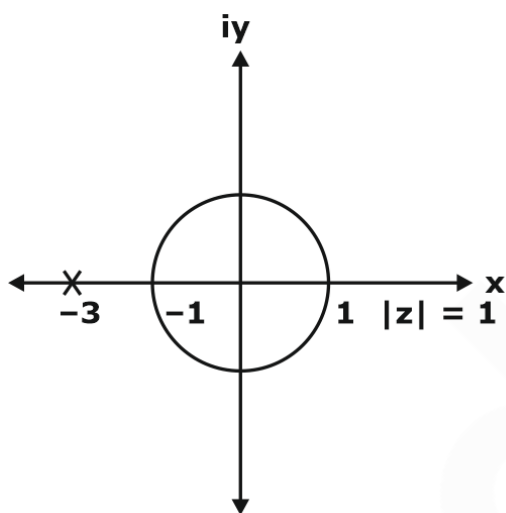
$$Z^2 + 6Z + 9 = 0$$

$$(Z + 3)^2 = 0$$

$$Z_1 = Z_2 = -3$$

$$C : |z| = 1$$

\Rightarrow unit circle (centre at (0, 0) and radius = 1)



Both the poles are outside 'c': $|z| = 1$

\therefore No – singular points

$\therefore f(z)$ is completely analytic function

By Cauchy's integral theorem

$$\oint_C f(z) \cdot dz = 0$$

25. $f(z) = (z - 1)^{-1} - 1 + (z - 1) - (z - 1)^2 + \dots$ is series expansion of

A. $\frac{-1}{z(z-1)}$, for $|z - 1| < 1$

B. $\frac{1}{z(z-1)}$, $|z - 1| < 1$

C. $\frac{-1}{z-1}$, for $|z - 1| < 1$

D. $\frac{1}{(z-1)^2}$, for $|z - 1| < 1$

Ans. B

Sol $f(z) = (z - 1)^{-1} - 1 + (z - 1) - (z - 1)^2 + (z - 1)^3 - \dots$

$$f(z) = (z - 1)^{-1} - [1 - (z - 1) + (z - 1)^2 - (z - 1)^3 + \dots]$$

$$f(z) = (z - 1)^{-1} [1 + (z - 1)]^{-1}$$

$$f(z) = (z - 1)^{-1} - z^{-1}$$



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$$f(z) = \frac{1}{z-1} - \frac{1}{z}$$

$$f(z) = \frac{z - (z-1)}{z(z-1)}$$

$$f(z) = \frac{1}{z(z-1)}; |z-1| < 1$$

26. Given $A = \begin{pmatrix} 2 & 5 \\ 0 & 3 \end{pmatrix}$

The value of the determinant of
 $|A^4 - 5A^3 + 6A^2 + 2I|$

Sol. Given $A = \begin{bmatrix} 2 & 5 \\ 0 & 3 \end{bmatrix}$

Eigen values of A are 2, 3

$$\text{Let } f(A) = A^4 - 5A^3 + 6A^2 + 2I$$

$$f(\lambda) = \lambda^4 - 5\lambda^3 + 6\lambda^2 + 2$$

\therefore Eigen values of $f(A)$ are $f(2)$ and $f(3)$

$$\text{i.e. } 1 \text{ and } f(2) = 2^4 - 5 \times 2^3 + 6 \times 2^2 + 2 = 16$$

$$= 16 - 40 + 24 + 2$$

$$f(2) = 2$$

$$f(3) = 3^4 - 5 \times 3^3 + 6 \times 3^2 + 2$$

$$f(3) = 81 - 135 + 54 + 2$$

$$f(3) = 2$$

Now,

$$|A^4 - 5A^3 + 6A^2 + 2I|$$

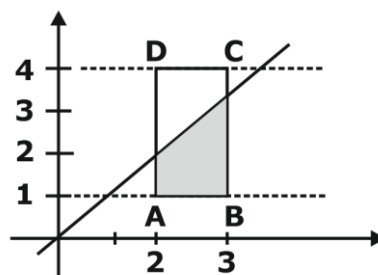
$$= |f(A)| = f(2) \cdot f(3)$$

$$= 4$$

27. Consider X and Y are independent continuous valued random variables with uniform PDF given by $X \sim U(2, 3)$ and $Y \sim U(1, 4)$. Then $P(Y \leq X)$ is

Sol. X and Y are uniformly distributed

$$X \sim U(2, 3) \text{ and } Y \sim U(1, 4)$$



$$P(Y \leq X) = \frac{\text{Shaded Area}}{\text{Total area of rectangle ABCD}}$$

$$= \frac{\frac{1}{2}(1+2) \times 1}{1 \times 3}$$

$$= \frac{3/2}{3}$$

$$= \frac{1}{2} = 0.5$$

28. Consider row vectors

$$U(1, 0), W = (2, 0)$$

Sol. $2U^T U + 3 W^T W$

$$= 2 \begin{bmatrix} 1 \\ 0 \end{bmatrix} \begin{bmatrix} 1 & 0 \end{bmatrix} + 3 \begin{bmatrix} 2 \\ 0 \end{bmatrix} \begin{bmatrix} 2 & 0 \end{bmatrix}$$

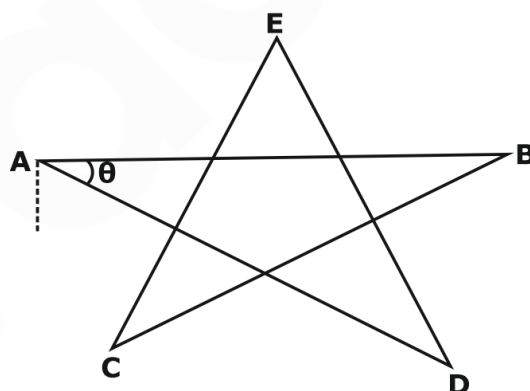
$$= 2 \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} + \begin{bmatrix} 4 & 0 \\ 0 & 0 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & 0 \\ 0 & 0 \end{bmatrix} + \begin{bmatrix} 12 & 0 \\ 0 & 0 \end{bmatrix}$$

$$M = \begin{bmatrix} 14 & 0 \\ 0 & 0 \end{bmatrix} = \text{Echelon form}$$

29. $\theta = ?$

$$AB = BC = CD = DE = EA$$



A. 36

B. 45

C. 72

D. 108

Ans. A

ME | CE | EE | EC | CS

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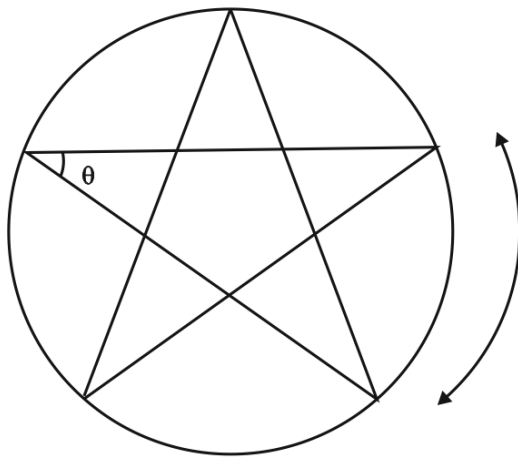
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Sol. Given $AB = BC = CD = DE = EA$

Known as regular star

The vertices of regular star lies on a circle



Angle of this arc at centre = 2θ
So, length = $(2\theta)r$

$$(2\theta \times r) \times 5 = \text{circumference} = 2\pi r$$

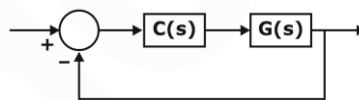
$$\Rightarrow \theta \times 5 = \pi$$

$$\Rightarrow \theta = \frac{\pi}{5} = 36^\circ$$

30. Consider a unity feedback configuration with a plant and a P.D controller shown in figure

$$G(s) = \frac{1}{(s+1)(s+3)} \text{ \& } c(s) = \frac{K(s+3-j)(s+3+j)}{s}$$

With k being scalar. The closed loop is?



A. only stable for $K > 0$

B. only stable for k between -1 and +1.

C. stable for all value of K

D. only stable for $K < 0$

Ans. A

Sol. $1 + G(s)C(s) = 0$

$$1 + \frac{1}{(s+1)(s+3)} \times \frac{k(a+3-j)(s+3+j)}{s}$$

$$s(s^2 + 4s + 3) + k[s^2 + 6s + 9 + 1] = 0$$

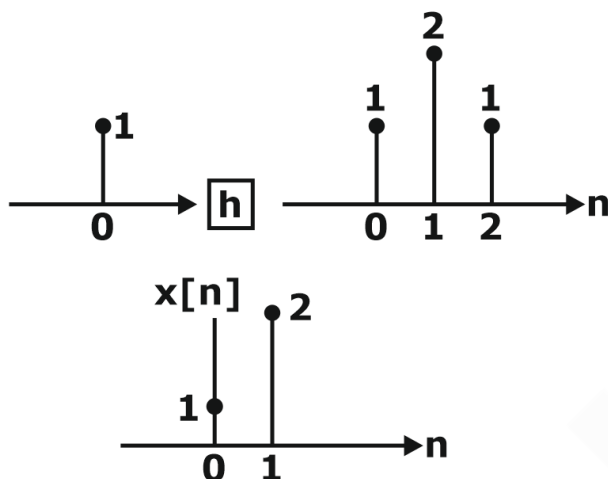
$$s^3 + (4+k)s^2 + s(6k+3) + 10k = 0$$

No, need to go for routh area

As according to necessary condition, all coefficients must be of same sign

So, $k > 0 \rightarrow$ only options (a) matches.

31. Input-output relationship of LTI system is shown below
The peak value of output when $x(n)$ is passed through it, is



- A. 4
- B. 5
- C. 2
- D. 6

Ans. B

Sol. The given output is output for impulse input, i.e. impulse response $h(n)$.

Now, Output for input $x(n)$

Will be $y(n) = x(n) * h(n)$

	1	2	1	
1	1	2	1	
2		2	4	2
	1	4	5	2

So peak value = 5



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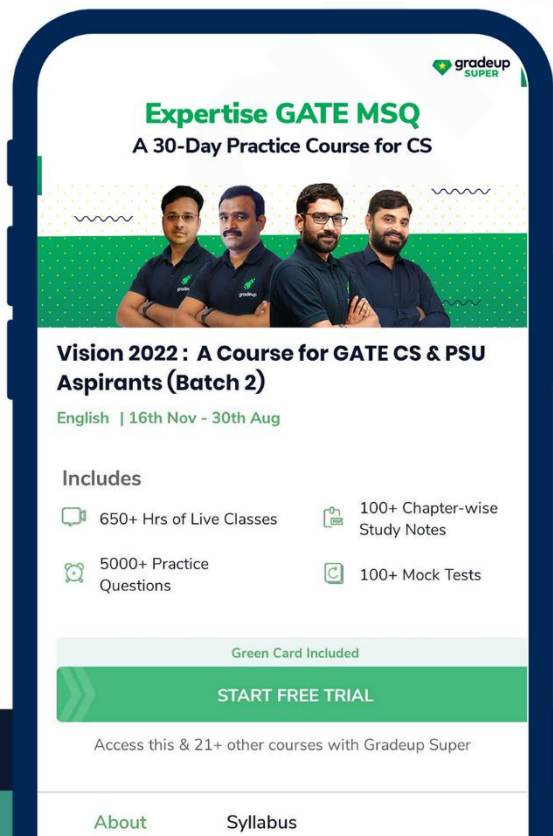
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