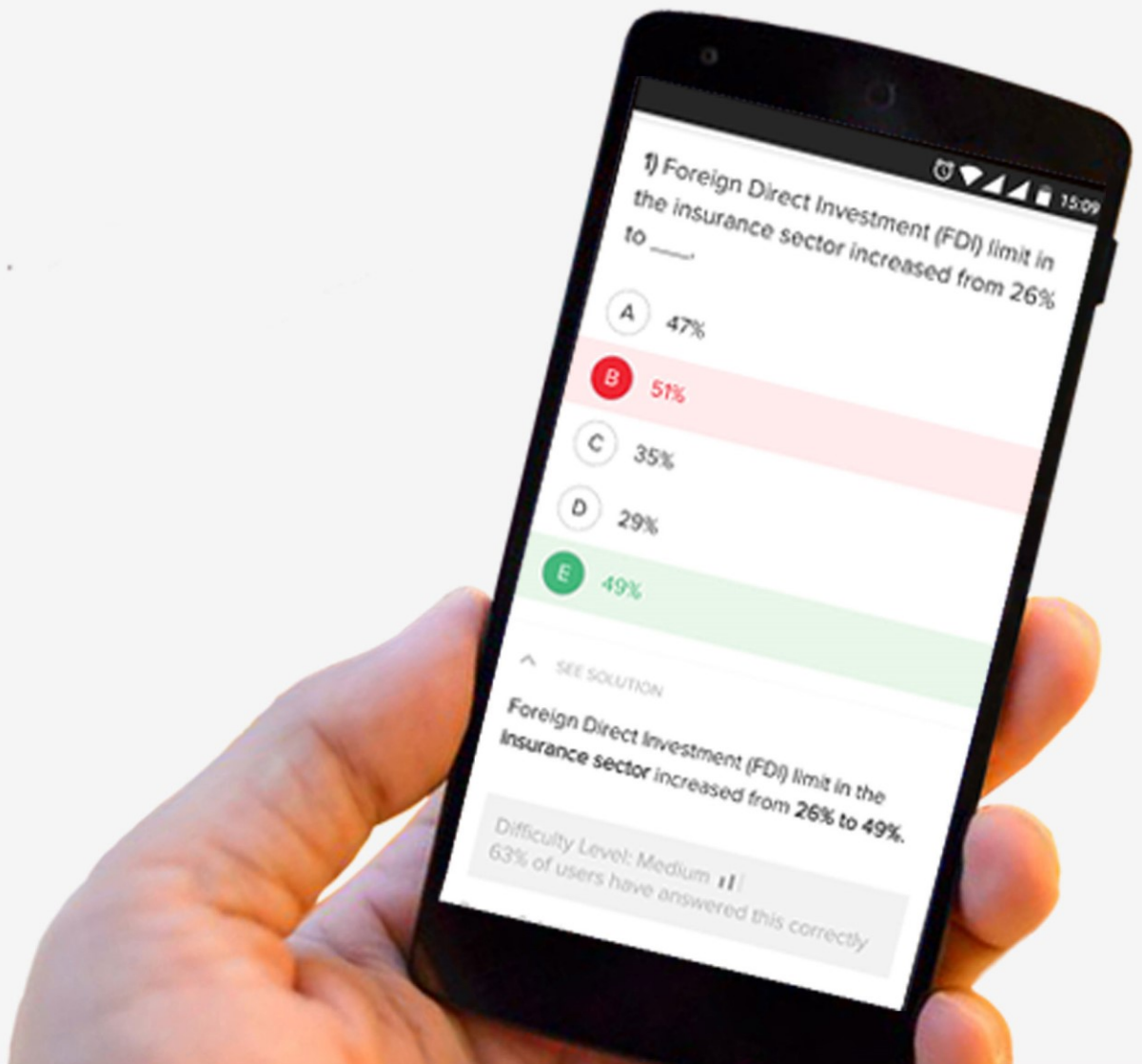




Formulas on Digital Communication for GATE EC Exam



Digital Communication

Matched filter:

→ impulse response $a(t) = P^*(T-t) \cdot P(t) \rightarrow i/p$

→ Matched filter o/p will be max at multiples of 'T'. So, sampling @ multiples of 'T' will give max SNR (2nd point)

→ matched filter is always causal $a(t) = 0$ for $t < 0$

→ Spectrum of o/p signal of matched filter with the matched signal as i/p ie, except for a delay factor ; proportional to energy spectral density of i/p.

$$\phi_0(f) = H_{opt}(f) \phi(f) = \phi(f) \phi^*(f) e^{-2\pi f T}$$

$$\phi_0(f) = |\phi(f)|^2 e^{-j2\pi f T}$$

→ o/p signal of matched filter is proportional to shifted version of auto correlation fine of i/p signal

$$\phi_0(t) = R_\phi(t-T)$$

At $t = T$ $\phi_0(T) = R_\phi(0) \rightarrow$ which proves 2nd point

Cauchy-Schwartz in equality :-

$$\left| \int_{-\infty}^{\infty} g_1^*(t) g_2(t) dt \right|^2 \leq \int_{-\infty}^{\infty} g_1^2(t) dt \int_{-\infty}^{\infty} |g_2(t)|^2 dt$$

If $g_1(t) = c g_2(t)$ then equality holds otherwise ' $<$ ' holds

Raised Cosine pulses :

$$P(t) = \frac{\sin\left(\frac{\pi t}{T}\right)}{\left(\frac{\pi t}{T}\right)} \cdot \frac{\cos\left(\frac{\pi \alpha t}{T}\right)}{1-4\alpha^2 t^2 T^2}$$

$$P(f) = \begin{cases} T, & |f| \leq \frac{1-\alpha}{2T} \\ T \cos^2\left(\frac{\pi t}{2\alpha}\left(|f| - \frac{1-\alpha}{2T}\right)\right); & \frac{1-\alpha}{2T} \leq |f| \leq \frac{1+\alpha}{2T} \\ 0, & |f| > \frac{1+\alpha}{2T} \end{cases}$$

- Bandwidth of Raised cosine filter $f_B = \frac{1+\alpha}{2T} \Rightarrow$ Bit rate $\frac{1}{T} = \frac{2f_B}{1+\alpha}$
 $\alpha \rightarrow$ roll of factor
 $T \rightarrow$ signal time period

→ For Binary PSK $P_e = Q\left(\frac{d}{2\sigma}\right) = Q\left(\sqrt{\frac{2\epsilon_s}{N_0}}\right) = \frac{1}{2} \operatorname{erfc}\left(\sqrt{\frac{\epsilon_s}{N_0}}\right)$.

→ 4 PSK $P_e = 2Q\left(\sqrt{\frac{2\epsilon_b}{N_0}}\right) \left[1 - \frac{1}{2} Q\left(\sqrt{\frac{2\epsilon_b}{N_0}}\right)\right]$

FSK:-

For BPSK

$$P_e = Q\left(\frac{d}{2\sigma}\right) = Q\left(\sqrt{\frac{\epsilon_s}{N_0}}\right) = \frac{1}{2} \operatorname{erfc}\left(\sqrt{\frac{\epsilon_s}{2N_0}}\right)$$

→ All signals have same energy (Const energy modulation)

→ Energy & min distance both can be kept constant while increasing no. of points . But Bandwidth Comprised.

→ PPM is called as Dual of FSK .

→ For DPSK $P_e = \frac{1}{2} e^{-\epsilon_b/N_0}$

→ Orthogonal signals require factor of '2' more energy to achieve same P_e as anti podal signals

→ Orthogonal signals are 3 dB poorer than antipodal signals. The 3dB difference is due to distance b/w 2 points.

→ For non coherent FSK $P_e = \frac{1}{2} e^{-\epsilon_b/N_0}$

→ FPSK & 4 QAM both have comparable performance .

→ 32 QAM has 7 dB advantage over 32 PSK.

- Bandwidth of Mary PSK $= \frac{2}{T_s} = \frac{2}{T_b \log_2^m}$; $S = \frac{\log_2^m}{2}$
- Bandwidth of Mary FSK $= \frac{M}{2T_s} = \frac{M}{2T_b \log_2^m}$; $S = \frac{\log_2^m}{m}$
- Bandwidth efficiency $S = \frac{R_b}{B.W}$.
- Symbol time $T_s = T_b \log_2^m$
- Band rate $= \frac{\text{Bit rate}}{\log_2^m}$



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